

ENG 382 ASSIGNMENT 2

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DEPARTMENT: MECHANICAL ENGINEERING

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$

$$f(x) = e^{-0.5x} (4x) - 2$$

$$f'(x) = u = e^{-0.5x} \quad v = 4 - x$$

$$f'(x) = \frac{dy}{dx} = \frac{v dy}{dx} + \frac{u dv}{dx}$$

$$f'(x) = (4-x)(-0.5e^{-0.5x}) + e^{-0.5x}(4)$$

$$f'(x) = 0.5e^{-0.5x}(4-x) - e^{-0.5x}$$

$$x_{n+1} = x_n - \frac{e^{-0.5x} (4x) - 2}{0.5e^{-0.5x} (4-x) - e^{-0.5x}}$$

i	x	E _i
0	0.5	0
1	0.838890606	40.3921204
2	0.8849559109	0.305386019
3	0.8957066071	0.05497707201
4	0.895706602	

$$x_{0+1} = \frac{0.5 e^{-0.5(0.5)} (4 - 0.5) - 2}{e^{-0.5(0.5)} (0.5 - 4) - e^{-0.5 \times 0.5}}$$

$$= 0.838890606$$

$$E_0 \% \text{ error} = \left| \frac{x_{n+1} - x_n}{x_{n+1}} \right| \times 100\%$$

$$= \left| \frac{0.838890606 - 0.5}{0.838890606} \right| \times 100$$

$$= 40.39747299$$

$$x_2 = 0.838890606 - \frac{e^{-0.5(0.838890606)} (4 - 0.838890606) - 2}{0.5 e^{-0.5(0.838890606)} (0.838890606 - 4) - e^{-0.5(0.838890606)}}$$

$$= 0.8849559809$$

$$E_1 = \left| \frac{0.8849559809 - 0.838890606}{0.8849559809} \right| \times 100$$

$$= 5.205386019$$

$$x_3 = 0.8849559809 - \frac{e^{-0.5(0.8849559809)} (4 - 0.8849559809) - 2}{0.5 e^{-0.5(0.8849559809)} (0.8849559809 - 4) - e^{-0.5(0.8849559809)}}$$

$$= 0.8857086071$$

$$K_3 = \left| \frac{0.8857086071 - 0.7849559804}{0.8857086071} \right| \times 100$$

$$= 0.8497447061$$

$$K_4 = \frac{0.8857086071 - e^{-0.5(0.8857086071)}}{0.5 e^{-0.5(0.8857086071)}} \frac{(4 - 0.8857086071) - 2}{(4 - 0.8857086071) - 4}$$

$$= 0.885708802$$

$$K_5 = \left| \frac{0.885708802 - 0.8857086071}{0.885708802} \right| \times 100$$

$$= 2.200997405 \times 10^{-5}$$