

Assignment 2  
17/ENG021028

SHAFIQ PRANCS  
COMPUTER ENGINEERING

1.  $F = x^2 \hat{i} + (3x + 2) \hat{j} + \sin x \hat{k}$

a.  $\frac{dF}{dx} = 2x \hat{i} + 3 \hat{j} + \cos x \hat{k}$

b.  $\frac{d^2F}{dx^2} = 2 \hat{i} - \sin x \hat{k}$

c.  $\left| \frac{dF}{dx} \right| = \text{at } 1 = 2(1) \hat{i} + 3 \hat{j} + \cos(1) \hat{k}$   
 $= 2 \hat{i} + 3 \hat{j} + 0.999 \hat{k}$   
 $= \sqrt{2^2 + 3^2 + (0.999)^2}$   
 $= \sqrt{13.998}$   
 $= 3.74$

$\frac{d(F \cdot F)}{dx} = (x^2 \hat{i} + (3x+2) \hat{j} + \sin x \hat{k}) \cdot (x^2 \hat{i} + (3x+2) \hat{j} + \sin x \hat{k}) - (x^2 + (3x+2)^2 + \sin^2 x)$   
 $= x^4 + 9x^2 + 12x + 4 + \sin^2 x$

$\frac{d(\sin^2 x)}{dx} = \sin^2 x = \sin x \cos x$       $u = \sin x$       $v = \sin x$   
 $\frac{du}{dx} = \cos x$       $\frac{dv}{dx} = \cos x$

Using Product rule

$$U \frac{dv}{dx} + V \frac{du}{dx}$$

$$= \sin(\cos x) + \sin(\cos x)$$

$$\sin x \cos x + \sin x \cos x$$

$$\frac{d}{dx}(\sin^2 x) = 2 \sin x \cos x$$

$$\frac{d}{dx}(F \cdot F) = 4x + 18x + 12 + 2 \sin x \cos x$$

at  $x = 1$

$$= 4(1) + 18(1) + 12 + \sin(1) \cos(1)$$

$$= 4 + 18 + 12 + 0.03484$$

$$= 34.03$$