

OLUYEMI Israel Amosluwapo -
16/ENG06/057.
Mechanical Engg.
Eng 382

Assignment (3)

Estimate the value of temp. using Gauss elimination method.

$$\begin{aligned} T_1 + T_2 - 2T_3 + T_4 + 3T_5 - T_6 &= 4 \\ 2T_1 - T_2 + T_3 + 2T_4 + T_5 - 3T_6 &= 20 \\ T_1 + 3T_2 - 3T_3 - T_4 + 2T_5 + T_6 &= -15 \\ 5T_1 + 2T_2 - T_3 - T_4 + 2T_5 + T_6 &= -3 \\ -3T_1 - T_2 + 2T_3 + 3T_4 + T_5 + 3T_6 &= 16 \\ 4T_1 + 3T_2 + T_3 - 6T_4 - 3T_5 - 2T_6 &= -27 \end{aligned}$$

In Matrix form;

$$\begin{bmatrix} 1 & -2 & 1 & 3 & -1 & 3 \\ 2 & -1 & 1 & 2 & 1 & -3 \\ 1 & 3 & -3 & -1 & 2 & 1 \\ 5 & 2 & -1 & -1 & 2 & 1 \\ -3 & -1 & 2 & 3 & 1 & 3 \\ 4 & 3 & 1 & 6 & 3 & -2 \end{bmatrix} \begin{bmatrix} T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \end{bmatrix} = \begin{bmatrix} 4 \\ 20 \\ -15 \\ -3 \\ 16 \\ -27 \end{bmatrix}$$

Using Gauss elimination Method.

Row $r_2 = \text{row } 1$, Pivot element first element in row

$$\therefore f_1 = 2/1, f_2 = 1/1, f_3 = 1/1, f_4 = -3/1, f_5 = 4/1$$

$$\begin{bmatrix} 1 & -2 & 1 & 3 & -1 & 3 \\ 2-2(1) & -1-2(-2) & 1-2(1) & 2-2(3) & 1-2(-1) & -3-2(3) \\ 1-1(1) & 3-1(-2) & -3-1(1) & -1-1(3) & 2-1(2) & 1-1(1) \\ 5-5(1) & 2-5(-2) & -1-5(1) & -1-5(3) & 2-5(-1) & 1-5(1) \\ -3-(-3)(1) & -1-(-3)(-2) & 2-(-3)(1) & 3-(-3)(3) & 1-(-3)(-1) & 3-(-3)(3) \\ 4-4(1) & 3-4(-2) & 1-4(1) & 6-4(3) & 3-4(-1) & -2-4(3) \end{bmatrix}$$

$$\begin{array}{c}
 \left[\begin{array}{cccccc}
 1 & 1 & -2 & 1 & 3 & -1 \\
 2-(2(1)) & -1-(2(1)) & 1-(2(-2)) & 1-(2(1)) & 3 & -1 \\
 1-(4(1)) & 3-(4(1)) & 3-(1(-2)) & -1-(1(1)) & 1-(2(3)) & -3(2(-1)) \\
 5-(5(1)) & 2-(5(1)) & -1-(5(-2)) & -1-(5(1)) & 2-(1(3)) & 1-(1(-1)) \\
 3-(3(1)) & -1-(3(1)) & 2-(3(-2)) & 3-(3(1)) & 2-(5(3)) & 1-(5(-1)) \\
 4-(4(1)) & 3-(4(1)) & 1-(4(-2)) & 3-(3(1)) & 1-(3(3)) & 3-(3(-1)) \\
 4-(4(1)) & 3-(4(1)) & 1-(4(-2)) & 3-(3(1)) & 1-(3(3)) & 3-(3(-1)) \\
 4-(4(1)) & 3-(4(1)) & 1-(4(-2)) & 3-(3(1)) & 1-(3(3)) & 3-(3(-1))
 \end{array} \right]
 \begin{array}{c}
 T_1 \\
 T_2 \\
 T_3 \\
 T_4 \\
 T_5 \\
 T_6
 \end{array}
 =
 \begin{array}{c}
 4 \\
 20-(2(4)) \\
 -15-(1(4)) \\
 -3-(5(4)) \\
 16-(3(4)) \\
 -22-(4(4))
 \end{array}
 \end{array}$$

$$\left[\begin{array}{cccccc}
 1 & 1 & -2 & 1 & 3 & -1 \\
 0 & -3 & 5 & 0 & -5 & -1 \\
 0 & 2 & -1 & -2 & -1 & 2 \\
 0 & -3 & 9 & -6 & -13 & 6 \\
 0 & 2 & -4 & 6 & 10 & 0 \\
 0 & -1 & 9 & -10 & -15 & 2
 \end{array} \right]
 \begin{array}{c}
 T_1 \\
 T_2 \\
 T_3 \\
 T_4 \\
 T_5 \\
 T_6
 \end{array}
 =
 \begin{array}{c}
 4 \\
 12 \\
 -19 \\
 -23 \\
 28 \\
 -13
 \end{array}$$

Pivot row is row 2; Pivot element is 2nd element in row 2
 $f_1 = 2/-3$, $f_2 = -3/-3 = 1$, $f_3 = 2/-3$, $f_4 = -1/-3 = 1/3$.

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & -3 & 5 & 0 & -5 & -1 \\ 0 & 0 & 1 - (2/3)(-2) & -2(2/3)(6) & -1(-2/3)(-5) & 2(-2/3)(-1) \\ 0 & 0 & 9 - (1)(5) & -6 - (1)(6) & -13 - (1)(5) & -6 - (1)(-1) \\ 0 & 0 & -4(-2/3)(5) & 6(-2/3)(6) & 16 - (-2/3)(-5) & 0 - (-2/3)(-1) \\ 0 & 0 & 9 - (5)(1/3) & -10 - (1/3)(6) & -15 - (1/3)(-5) & 2 - (1/3)(-1) \end{bmatrix} \begin{matrix} T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \end{matrix} = \begin{bmatrix} 4 \\ 12 \\ -11 \\ -35 \\ 36 \\ 47 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & -3 & 5 & 0 & -5 & -1 \\ 0 & 0 & 4/3 & -2 & -13/3 & 4/3 \\ 0 & 0 & 4 & -6 & -8 & 7 \\ 0 & 0 & -2/3 & 6 & 20/3 & -2/3 \\ 0 & 0 & 22/3 & -10 & -4/3 & 2/3 \end{bmatrix} = \begin{bmatrix} 4 \\ 12 \\ -11 \\ -35 \\ 36 \\ 47 \end{bmatrix}$$

Row 2; $f_1 = 4/(4/3) = 12/7$, $f_2 = -2/3 \div (-4/3) = 2/7$, $f_3 = 22/3$

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & -3 & 5 & 0 & -5 & -1 \\ 0 & 0 & 4/3 & -2 & -13/3 & 4/3 \\ 0 & 0 & 4 - (12/7)(4/3) & -6 - (12/7)(-2) & -8 - (12/7)(-13/3) & 7 - (12/7)(4/3) \\ 0 & 0 & -2/3 + (2/7)(4/3) & 6 + (2/7)(-2) & 20/3 + 2/7(-13/3) & -2/3 + 2/7(4/3) \\ 0 & 0 & 22/3 - 22/7(4/3) & -10 - (22/7)(-2) & -4/3 - 22/7(-13/3) & 2/3 - 22/7(4/3) \end{bmatrix} \begin{matrix} T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \end{matrix} = \begin{bmatrix} 4 \\ 12 \\ -11 \\ 35 - 12/f_1 \\ 36 - 2/f_2 \\ 47 - 22/f_3 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & -3 & 5 & 0 & -5 & -1 \\ 0 & 0 & 2/3 & -2 & -13/3 & 4/3 \\ 0 & 0 & 0 & -18/7 & -4/7 & 33/7 \\ 0 & 0 & 0 & 38/7 & 38/7 & 2/7 \\ 0 & 0 & 0 & -26/7 & -26/7 & -13/7 \end{bmatrix} \begin{matrix} T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \end{matrix} = \begin{bmatrix} 4 \\ 12 \\ -11 \\ -113/7 \\ 238/7 \\ -82/7 \end{bmatrix}$$

First row is row 4.

First element is fourth element on row 4

$$f_1 = 38/7 \div (-18/7) = -38/18 = -19/9$$

$$f_2 = -26/7 \div (-18/7) = 26/18 = 13/9$$

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & -3 & 5 & 0 & -5 & -1 \\ 0 & 0 & 2/3 & -2 & -15/3 & 4/3 \\ 0 & 0 & 0 & -18/7 & -4/7 & 33/7 \\ 0 & 0 & 0 & 38/7 + (19/9 \times -18/7) & 38/7 + (19/9 \times -4/7) & 2/7 + (19/9 \times 33/7) \\ 0 & 0 & 0 & -26/7 + (13/9 \times -18/7) & -26/7 + (13/9 \times -4/7) & -13/7 + (13/9 \times 33/7) \end{bmatrix} \begin{matrix} T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \end{matrix} = \begin{bmatrix} 4 \\ 12 \\ -11 \\ -113/7 \\ \frac{230}{7} - \left(-\frac{113}{7} \times \frac{19}{9}\right) \\ -\frac{82}{7} - \left(-\frac{113}{7} \times \frac{13}{9}\right) \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & -3 & 5 & 0 & -5 & -1 \\ 0 & 0 & 2/3 & -2 & -13/3 & 4/3 \\ 0 & 0 & 0 & -18/7 & -4/7 & 33/7 \\ 0 & 0 & 0 & 0 & 38/9 & 29/3 \\ 0 & 0 & 0 & 0 & 10/9 & -26/3 \end{bmatrix} \begin{matrix} T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \end{matrix} = \begin{bmatrix} 4 \\ 12 \\ -11 \\ -113/7 \\ -11/9 \\ 98/9 \end{bmatrix}$$

First row is row 5.

$$f_1 = 10/9 \div 38/9 = 10/38$$

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & -3 & 5 & 0 & -5 & -1 \\ 0 & 0 & 2/3 & -2 & -13/3 & 4/3 \\ 0 & 0 & 0 & -18/7 & -4/7 & 33/7 \\ 0 & 0 & 0 & 0 & 38/9 & 29/3 \\ 0 & 0 & 0 & 0 & 10/9 + \left(\frac{10}{38} \times \frac{38}{9}\right) & -26/3 + \left(\frac{10}{38} \times \frac{29}{3}\right) \end{bmatrix} \begin{matrix} T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \end{matrix} = \begin{bmatrix} 4 \\ 12 \\ -11 \\ -113/7 \\ -11/9 \\ 98/9 - \left(\frac{10}{38} \times \frac{11}{9}\right) \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & 2 & 1 & 3 & -1 \\ 0 & 3 & 5 & 0 & -5 & -1 \\ 0 & 0 & 2/3 & -2 & -13/3 & 4/3 \\ 0 & 0 & 0 & -18/7 & -4/7 & 33/7 \\ 0 & 0 & 0 & 0 & 38/9 & 29/3 \\ 0 & 0 & 0 & 0 & 0 & -213/19 \end{bmatrix} \begin{bmatrix} T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \end{bmatrix} = \begin{bmatrix} 4 \\ 12 \\ 11 \\ -113/7 \\ -11/9 \\ 213/19 \end{bmatrix}$$

Multiplying the matrix.

$$0 + (-213/19) T_6 = 213/19$$

$$19/213 \times 213/19 T_6 = 213/19 \times 19/213$$

$$T_6 = 1$$

$$T_6 = -1$$

$$\text{Also, } 0 + 38/9 T_5 + 29/3 T_6 = -11/9$$

$$\text{at } T_6 = -1$$

$$38/9 T_5 + 29/3 (-1) = -11/9$$

$$T_5 = \frac{26}{9} \div \left(\frac{38}{9} \right)$$

$$\rightarrow 2. \quad T_5 = 2$$

$$-18/7 T_4 - 4/7 T_5 + 33/7 T_6 = -113/7$$

$$\text{where } T_6 = -1, T_5 = 2$$

$$-18/7 T_4 - 4/7 (2) + 33/7 (-1) = -113/7$$

$$T_4 = -\frac{72}{7} \times 2/18$$

$$T_4 = 4$$

To get T_3

$$2/3 T_3 - 2T_4 - 13/3 T_5 + 4/3 T_6 = -11$$

$$-2/3 T_3 - 18 = -11$$

$$2/3 T_3 = -11 + 18$$

$$T_3 = 9 \times 3/4$$

$$\boxed{T_3 = 31}$$

To get T_2

$$3T_2 + 5T_3 - 5T_5 - T_6 = 12$$

$$-3T_2 + 5(3) + 0 - 5(2) + 1 = 12$$

$$-3T_2 + 6 = 12$$

$$\boxed{T_2 = -2}$$

To get T_1

$$T_1 + T_2 - 2T_3 + T_4 + 3T_5 - T_6 = 4$$

$$T_1 - 2 - 2(3) + 4 + 3(2) - (-1) = 4$$

$$T_1 = 4 - 3$$

$$\boxed{T_1 = 1}$$

Therefore;

$$\begin{bmatrix} T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \end{bmatrix} = \begin{bmatrix} 1 \\ -2 \\ 31 \\ 2 \\ 2 \\ -1 \end{bmatrix}$$