

Assignment 2

Given that $f = x^2 i + (3x+2) j + \sin x k$
 $\Rightarrow \frac{df}{dx} = 2xi + 3j + \cos x k$

$\Rightarrow \frac{d^2 f}{dx^2} = 2i - \sin x k$

$\left| \frac{df}{dx} \right|_{dx=1} = 2(1)^2 + 3^2 + (\cos(1))^2 = 2^2 + 3^2 + 1^2 = \sqrt{14}$

Q, $\left| \frac{df}{dx} \right| = \sqrt{2^2 + 3^2 + (\cos(1))^2} = \sqrt{4 + 9 + 0.99} = \sqrt{13.99} = 12$

$= (2x^2 i + (3x+2) j + \sin x k)$

1) $\frac{d(F \cdot F)}{dx} = F \cdot \frac{dF}{dx} + F \cdot \frac{dF}{dx}$

$(2x^2 i + (3x+2) j + \sin x k) \cdot (2xi + 3j + \cos x k) + (2x^2 i + (3x+2) j + \sin x k) \cdot (2xi + 3j + \cos x k)$
 $= 2x^3 + (9x+6) + (\cos x \sin x) + 2x^3 + 9x + 6 + \cos x \sin x$

$= 4x^3 + 18x + 12 + 2 \cos x \sin x$

2) If $r = (t^2 + 3t) i - 2 \sin 3t j + 3e^{2t} k$

a) $\Rightarrow \frac{dr}{dt} = (2t+3) i - 6 \cos 3t j + 6e^{2t} k$

b) $\Rightarrow \frac{d^2 r}{dt^2} = 2 i + 18 \sin 3t j + 12e^{2t} k$

The value

$$\left(\frac{d^2 r}{dt^2} \right) \text{ at } t = 0$$

$$= 2i + [8 \sin 3(0)] + 12e^{2(0)} = 2i + 0j + 12k = 2i + 12k$$

$$= \sqrt{2^2 + 12^2} = \sqrt{4 + 144} = \sqrt{148} = 12.165$$