

OMUYA ENEIRE GODWIN

Assignment 6

161 ENCS021047

COMPUTER ENGINEERING

ENCS382

Given:  $d = d\beta$  — (1)

Comparing eqn (1)

$$\log d = \log x + \log \beta$$

where  $a_0 = \log x$

$$a_1 = \log \beta$$

$y = \log x$	$x$	$xy$	$d(x)$	$x^2$	$y^2$
1. 0.301029996	2	0.602059992	2	4	0.09061905
2. 0.698970004	4	2.795880016	4	16	0.488551067
3. 1.278753601	8	10.230028808	8	64	1.63520742
4. 1.678970004	16	27.063520064	16	256	2.818940076
5. 2.178753601	32	70.120115232	32	1024	4.746940537
6. 2.678970004	64	171.074080256	64	4096	7.176940076
7. 3.178753601	128	407.060460224	128	16384	10.106940076
8. 3.678970004	256	937.034080512	256	65536	13.526940076
9. 4.178753601	512	2139.022048128	512	262144	17.466940076
10. 4.678970004	1024	4787.004096256	1024	1048576	21.886940076
11. 5.178753601	2048	10606.988192512	2048	4194304	26.816940076

$$\Sigma Y = 29.41137046$$

$$\Sigma X = 55$$

$$\Sigma XY = 199.8268839$$

$$\Sigma X^2 = 385$$

$$\Sigma Y^2 = 103.9620485$$

$$\Sigma Y = a_0 N + a_1 \Sigma X$$

$$29.41137046 = a_0(11) + a_1(55) \quad \text{--- (1)}$$

$$\Sigma XY = a_0 \Sigma X + a_1 \Sigma X^2$$

$$199.8268839 = a_0(55) + a_1(385) \quad \text{--- (2)}$$

solving eqn (1) & (2)

$$29.41137046 = 11a_0 + 55a_1$$

$$199.8268839 = 55a_0 + 385a_1$$

$$a_0 = \frac{\begin{vmatrix} 29.41137046 & 55 \\ 199.8268839 & 385 \end{vmatrix}}{\begin{vmatrix} 11 & 55 \\ 55 & 385 \end{vmatrix}}$$

$$\begin{vmatrix} 11 & 55 \\ 55 & 385 \end{vmatrix}$$

$$= \frac{(29.4133046)(885) - (55)(199.8268831)}{(11 \times 885) - (55 \times 55)}$$

$$d_0 = 0.27511$$

$$a_1 = \begin{vmatrix} 11 & 29.4133046 \\ 55 & 199.8268831 \end{vmatrix}$$

$$\begin{vmatrix} 11 & 55 \\ 55 & 885 \end{vmatrix}$$

$$a_1 = \frac{(11 \times 199.8268831) - (29.4133046 \times 55)}{[(11)(885)] - [55 \times 55]}$$

$$q_1 = 0.47973$$

$$\begin{aligned} \therefore q_0 &= \log \alpha \\ 0.2751 &= \log \alpha \\ \alpha &= 1.8841 \end{aligned}$$

$$\alpha = 1.8841$$

$$\beta = 3.0181$$

$$\begin{aligned} a_1 &= \log \beta \\ 0.47973 &= \log \beta \\ \beta &= 3.0181 \end{aligned}$$

## Correlation Coefficient

$$R = \frac{N \sum XY - (\sum X)(\sum Y)}{\sqrt{(N \sum X^2 - (\sum X)^2)(N \sum Y^2 - (\sum Y)^2)}}$$

$$R = \frac{(11 \times 199.8268839) - (55)(29.41133046)}{\sqrt{(11 \times 385 - 55^2) - [(11 \times 103.9425485 - (29.41133046)^2]}}$$

$$R = 0.9998448312$$

$$R^2 = (0.9998448312)^2$$
$$= 0.9996896864$$

For manual method,

$$R = 0.9998448312$$

$$R^2 = 0.9996896864$$

For Mat Lab

$$R = 0.9998$$

$$R^2 = 0.9997$$

For Excel,

$$R = 0.99984483235763$$

$$R^2 = 0.999689688792257$$

From observation for all the methods used to solve the correlation coefficient and its square, it can be seen that  $R^2 < R$ .