

Given  $d \propto \beta^t$  --- (1)

Comparing eqn (1) to  $y = mx + c$  to convert it into a linear equation.

$$\log d = \log \alpha + t \log \beta$$

$$y = a_0 + a_1 x$$

Therefore  $a_0 = \log \alpha$

$$a_1 = \log \beta$$

$$x = t$$

$$y = \log d$$

$Y = \log d$	$t = x$	$xY$	$d(x)$	$x^2$	$Y^2$
0.301029996	0	0	0	0	0.09061999
0.698970004	1	0.698970004	1	1	0.488357001
1.298753601	2	2.557507202	2	4	1.635211722
1.698970004	3	5.096910013	3	9	2.826457076
2.198970004	4	8.715907789	4	16	4.797740522
2.698970004	5	13.36048925	5	25	7.14066962
3.198970004	6	18.9411141	6	36	9.71571322
3.698970004	7	25.5058364	7	49	13.3541345
4.198970004	8	32.8944066	8	64	16.9068972
4.698970004	9	41.5269532	9	81	21.2899932
5.198970004	10	50.45405135	10	100	25.4561297

$$\sum Y = 29.41133046$$

$$\sum x = 55$$

$$\sum xY = 199.8268839$$

$$\sum x^2 = 385$$

$$\sum Y^2 = 102.9620485$$

$$2.7 = 10N + a_0 \cdot EK$$

$$29.41133046 = a_0(11) + a_1(55) \quad \text{--- (i)}$$

$$199.8268835 = 10C_{10} + a_0(55) + a_1(385) \quad \text{--- (ii)}$$

combining eqs (i) and (ii)

$$29.41133046 = 11a_0 + 55a_1$$

$$199.8268835 = 55a_0 + 385a_1$$

$$\begin{bmatrix} 29.41133046 & 55 \\ 199.8268835 & 385 \end{bmatrix}$$

$$\begin{bmatrix} 11 & 55 \\ 55 & 385 \end{bmatrix}$$

$$a_0 = \frac{[29.41133046][385] - [55][199.8268835]}{[11 \times 385] - [55 \times 55]} = 0.29511$$

$$a_1 = \begin{bmatrix} 11 & 29.41133046 \\ 55 & 199.8268835 \end{bmatrix}$$

$$\begin{bmatrix} 11 & 55 \\ 55 & 385 \end{bmatrix}$$

$$a_1 = \frac{[11 \times 199.8268835] - [29.41133046 \times 55]}{[11 \times 385] - [55 \times 55]}$$

$$a_1 = 0.47973$$

$$A_0 = \log \alpha$$

$$0.29511 = \log \alpha$$

$$\alpha = 1.9841$$

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$$A_1 = \log \beta$$

$$0.47293 = \log \beta$$

$$\beta = 3.0181$$

Correlation Coefficient.

$$r = \frac{N \sum XY - [\sum X][\sum Y]}{\sqrt{(N \sum X^2 - (\sum X)^2)[N \sum Y^2 - (\sum Y)^2]}}$$

$$r = \frac{[11 \times 199.8268839] - [55 \times 29.41133046]}{\sqrt{[11 \times 385 - 55^2] \times [(11 \times 103.960488)] - [29.41133046]^2}}$$

$$r = 0.9998448312$$

$R^2 = r^2$

$$R^2 = [0.9998448312]^2 = 0.9996896869$$

for manual method

$$R = 0.9998$$

$$R^2 = 0.9997$$

from excel

$$R = 0.99984483235763$$

$$R^2 = 0.999689688792257$$

D

From the values of Correlation Coefficient obtained manually above, it can be seen that the Correlation Coefficient ranges between 0.8 - 1 i.e. 0.9998. Therefore the variables  $\log d$  and  $t$  correlate effectively.