

Michael shallongwa

16/Eng01/019

Chemical Engineering

Maths assignment 6

$$d = \alpha \beta \dots (i)$$

Comparing eqn(i) to  $y = mx + c$

$$\log d = \log \alpha + \log \beta$$

$$a_0 = \log \alpha \text{ \& } a_1 = \log \beta \dots (ii)$$

$y = \log d$	$t = x$	$xy$	$d(m)$	$x^2$	$y^2$
0.30102996	0	0	0	0	0.09061905
0.69897004	1	0.69897004	1.0	1	0.488559067
1.278153601	2	2.55750	2	4	1.635210772
1.69897009	3	5.096910	3	9	2.88649976
2.178476947	4	8.71590	4	16	4.747940537
2.672097850	5	13.36049	5	25	7.140106962
3.1568519091	6	18.94111	6	36	9.96713925
3.543609011	7	25.58054	7	49	13.35441345
4.11800007	8	37.89440	8	64	16.4068993
4.614163911	9	44.52695	9	81	21.28997336
5.0454935	10	50.05005	10	100	25.4611297

$$\sum y = 29.91133046, \quad \sum x = 55, \quad \sum xy = 199.8268839$$

$$\sum x^2 = 385, \quad \sum y^2 = 103.9620485$$

$$\sum y^2 = a_0 N + a_1 \sum x$$

$$29.91133046 = a_0(11) + a_1(55)$$

$$\sum xy = a_0 \sum x + a_1 \sum x^2$$

$$199.8268839 = a_0(55) + a_1(385)$$

from eqn (i) & (ii)

$$a_0 = \begin{vmatrix} 29.91133046 & 55 \\ 199.8268839 & 385 \\ \hline 11 & 55 \\ 55 & 385 \end{vmatrix}$$

$$= \frac{(29.41133048 \times 385) - (55 \times 199 \times 8768538)}{(11 \times 385) \times (55 \times 55)}$$

$$a_0 = 0.77511$$

$$a_1 = \frac{\begin{vmatrix} 11 & 29.41133046 \\ 55 & 199.876835 \end{vmatrix}}{\begin{vmatrix} 11 & 55 \\ 55 & 385 \end{vmatrix}}$$

$$a_1 = 0.7973$$

$$\therefore a_1 = \log \beta \quad \therefore a_0 = 0.27511$$

$$\beta = 3.0181 \quad \alpha_0 = \log \alpha$$

$$\alpha = 1.8841$$

Correlation Coefficient

$$R = \frac{N \sum xy - (\sum x)(\sum y)}{\sqrt{N \sum x^2 - (\sum x)^2} \sqrt{N \sum y^2 - (\sum y)^2}}$$

$$R = 0.9998448312$$

$$R_{\text{square}} = 0.9996896864$$

Manual method:  $R = 0.9998448312$ ,  $R^2 = 0.999689686$

Mathlab:  $R = 0.9998$ ,  $R^2 = 0.9997$

excel:  $R = 0.9998448$ ,  $R^2 = 0.999689689$

from all the methods used to solve the correlation,  $R^2 < R$  in all the method used.