

17/ENGIN/021

Chemical ENGINEERING

ENG 282 ASSIGNMENT 5

(c)

$$\frac{dT}{dt} \propto (T - T_A)$$

$$\frac{dT}{dt} = k(T - T_A)$$

$$\frac{1}{T - T_A} dT = k \cdot dt$$

$$\ln(T - T_A) = kt + c$$

$$T - T_A = e^{kt+c}$$

$$T - T_A = e^{kt} \cdot e^c$$

$$T - T_A = e^{kt} \cdot T_0$$

$$T - T_A = T_0 e^{kt}$$

$$\text{@ } t = 0$$

$$25 - T_A = T_0 e^{k(0)}$$

$$25 - T_A = T_0$$

$$25 - 10 = T_0$$

$$\therefore T_0 = 15$$

$$T - T_A = 15e^{kt}$$

$$20 - 10 = 15e^{k(5)}$$

$$10 = 15e^{5k}$$

$$10/15 = e^{5k}$$

$$0.67 = e^{5k}$$

$$\ln 0.67 = 5k$$

$$\therefore k = \frac{\ln 0.67}{5} = -0.080$$

$$T - T_A = 15e^{-0.080(t)}$$

$$T - 10 = 15e^{-0.080(t)}$$

~~$$T = 10 + 15e^{-0.080(t)}$$~~

$$T = 10 + 15e^{-0.080(t)}$$

— model of the system.

(ii) MATLAB

Command window

clear

clc

close all

$$T = 10 + (15 * \exp*(-0.080 * t))$$

$$t = 0:1:60$$

$$T_n = \text{subs}(T)$$

Plot (t, T_n)

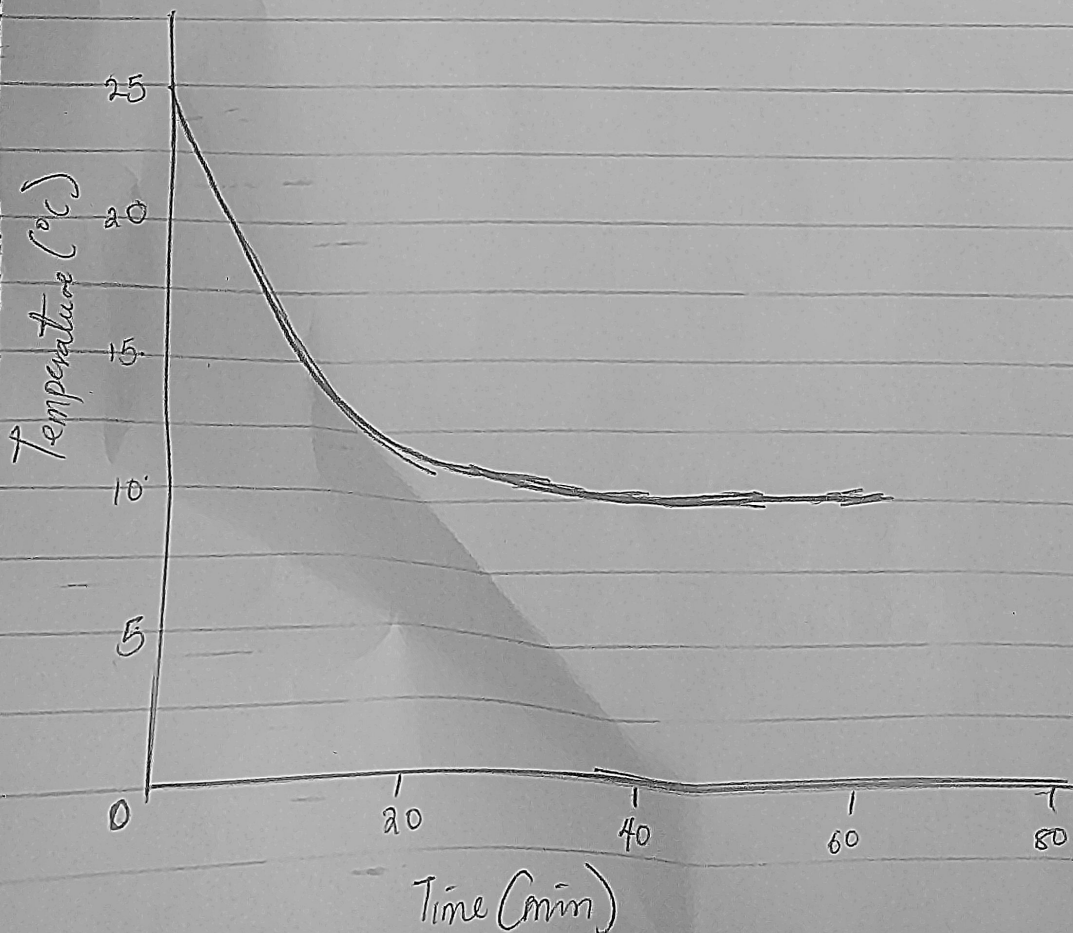
X label ('time (min)')

Y label ('Temperature (°C)')

grid on

grid minor

axis tight.



(iv) The steady-state temperature of the system is 10°C

~~$T = 10 + 15e^{...}$~~

(v) $T = 10 + 15e^{-0.080(t)}$

$T = 10 + 15e^{-0.080(60)}$

$T = 10 + 25$

$T = 25^{\circ}\text{C}$

(a) A mathematical model is a description of a system using mathematical concepts and language. The process of developing a mathematical model is termed mathematical modelling.

(b) System modelling language
life cycle modeling language