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Civil Engineering

17/ENG02/052

ENG 282

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a] Define Mathematically, Modelling.

Mathematically, modelling is a mathematical representation of a system and simulation of a system which involves solving the model and obtaining its output variable for different values of its input variable or as input variable is changed from one value to another

b] Methods of obtaining a model

- By the use of Balance Law
- By differentiating

c] i) Solution

$$T(0) = 10^{\circ}\text{C}$$

$$T(5) = 20^{\circ}\text{C}$$

$$\text{Actual temperature} = 25^{\circ}\text{C} = T_A$$

$$\frac{dT}{dt} = k(T - T_A)$$

$$dT = k(T - T_A) dt$$

$$k dt = \frac{dT}{(T - T_A)}$$

Integrating both sides

$$\ln(T - T_A) = kt + c$$

$$T - T_A = e^{kt} + e^c$$

Let  $e^c$  be A

$$T - T_A = e^{kt} \times A$$

$$T - T_A = Ae^{kt}$$

$$T = Ae^{kt} + T_A$$

When  $T = 10$

$$10 = A + 25$$

$$A = 10 - 25 = -15$$

$$T = 25 - 15e^{kt}$$

$$\text{At } t(s) = 20$$

$$20 = 25 - 15e^{kt}$$

$$20 - 25 = -15e^{k(5)}$$

$$-5 = -15e^{5k}$$

$$e^{5k} = \frac{-5}{-15}$$

$$= \frac{1}{3}$$

$$e^{5k} = 0.3333$$

$$5k = \ln(0.3333)$$

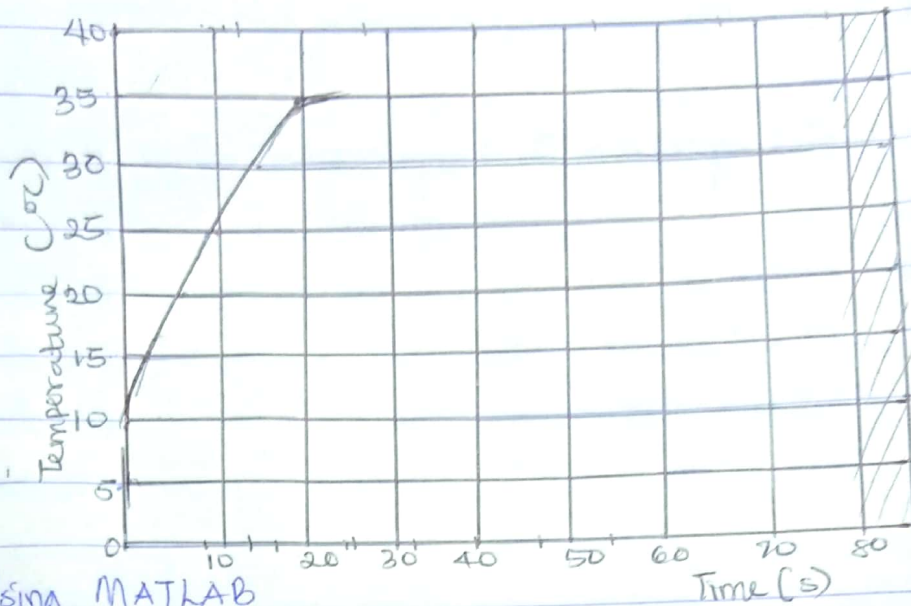
$$k = -0.22$$

$$\therefore (T(t) = 25 - 15e^{-0.22t}) \longrightarrow \text{Relating equation}$$

(ii) Using Microsoft Excel

- Pick a box, insert 't'
- Pick another box, insert 'T'
- Under the already labelled box 1 't'
- Insert a value of 0 in an empty box
- Go to
- Adjust click on series
- Insert a step value of 1
- Change the series into columns
- Insert a stop value of 60
- Under the already labelled box 2 'i'
- Pick a box
- Insert  $\rightarrow 25 - (15 * \text{EXP}(0.22 * A2))$
- Auto fill
- Go to insert
- Pick a graph of choice
- Label the graph

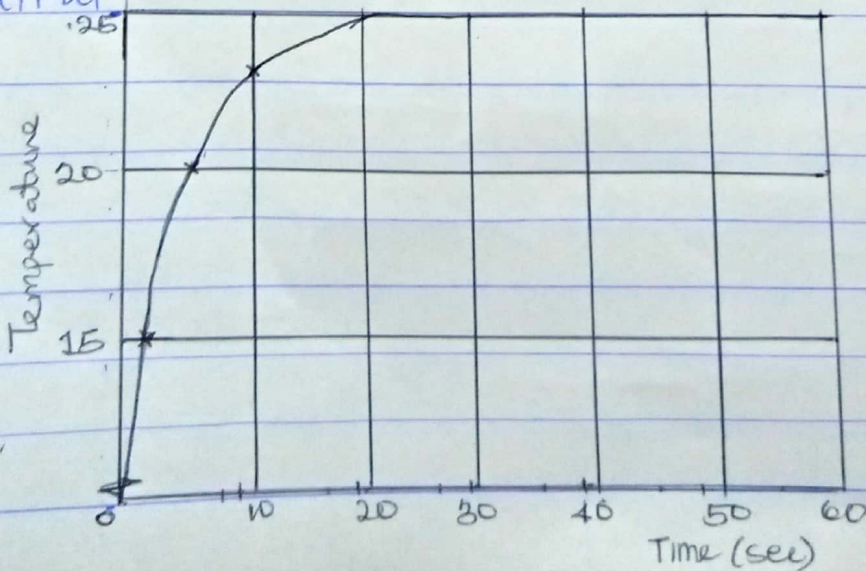
## OUTPUT



(iii) Using MATLAB

- Command window
- Clear
- Clc
- Close all
- $t = 0:1:60$
- $T = 25 - 15 * \exp(-0.22 * t)$
- Plot (t, T)
- Grid on
- Grid minor
- X Label ('Time (sec)')
- Y Label ('Temperature')

## OUTPUT



(iv) Using excel's dynamic response, State temperature of the system would be  $25^{\circ}\text{C}$  at 20 minutes.

(v) Using the developed model equation, the temperature of the thermometer at  $t$  will be  $25^{\circ}\text{C}$ .