

YAKUBU HEBRIMAT

17/ENG021050

COMPUTER ENGINEERING

Assignment 2

$$F = x^2 i + (3x+2) j + \sin x k$$

$$a) \frac{\partial F}{\partial x} = 2x i + 3j + \cos x k$$

$$b) \frac{\partial^2 F}{\partial x^2} = 2i - \sin x k$$

$$c) \left| \frac{\partial F}{\partial x} \right|_{x=1} = 2(1) i + 3j + (\cos 1) k \\ = 2i + 3j + 0.999 k$$

$$= \sqrt{2^2 + 3^2 + 0.999^2}$$

$$= \sqrt{13.958}$$

$$\approx 3.74$$

$$d) \frac{d}{dx} (F \cdot F)$$

$$(F \cdot F) = (x^2 i + (3x+2) j + \sin x k)^2$$

$$= (x^2 i + (3x+2) j + \sin x k) \cdot (x^2 i + (3x+2) j + \sin x k)$$

$$\frac{d(\sin^2 x)}{dx} = \sin^2 x = \sin x - \sin^2 x$$

$$u = \sin x, \quad v = \sin x$$
$$\frac{du}{dx} = \cos x, \quad \frac{dv}{dx} = \cos x$$

Product Rule

$$u \frac{dv}{dx} + v \frac{du}{dx}$$

$$\sin x (\cos x) + \sin x (\cos x)$$

$$\sin x \cos x + \sin x \cos x$$

$$\sin 2x = 2 \sin x \cos x$$

$$\frac{d}{dx} (F \cdot F) = 4x + (8x + 12 + 2 \sin \cos x)$$

$$\text{at } x = 1$$

$$= 4(1) + (8(1) + 12 + 2 \sin(1) \cos(1))$$

$$= 34.03$$