

AGDANIRU ROSEMARY

1712001/003

CHEMICAL ENGINEERING

ASSIGNMENT V SOLUTION

$$a) \frac{dT}{dt} = k(T - T_A)$$

$$\int \frac{1}{T - T_A} dT = \int k dt$$

$$\ln(T - T_A) = kt + c$$

$$T - T_A = e^{kt+c}$$

$$T - T_A = e^{kt} \cdot e^c$$

$$T - T_A = T_0 e^{kt}$$

$$T = T_A + T_0 e^{kt}$$

when $t = 0$

$$10 = 25 + T_0 e^{k(0)}$$

$$10 = 25 + T_0$$

$$T_0 = 10 - 25 = -15$$

$$T_0 = -15$$

$$T(t) = 25 - 15e^{kt}$$

$$\text{at } t(5) = 20^\circ$$

$$20 = 25 - 15e^{k(5)}$$

$$15e^{k(5)} = 25 - 20$$

$$15e^{k(5)} = 5$$

$$e^{k(5)} = \frac{5}{15}$$

$$e^{5k} = 0.3333$$

$$5k = \ln 0.33$$

$$5k = -1.0986$$

$$k = -0.2197$$

$$T(t) = 25 - 15 \exp^{-0.2197t}$$

Microsoft Excel

$$\begin{aligned} 10 &= 25 - (15 \cdot \exp(-0.2197 \cdot a_2)) \\ 12.95 &= 25 - (15 \cdot \exp(-0.2197 \cdot a_3)) \\ 15.33 &= 25 - (15 \cdot \exp(-0.2197 \cdot a_4)) \\ 17.240 &= 25 - (15 \cdot \exp(-0.2197 \cdot a_5)) \end{aligned}$$

iii Command window

clear

close

close

t=0:1:60

$$y = 25 - 15 \cdot \exp(-0.2197 \cdot t)$$

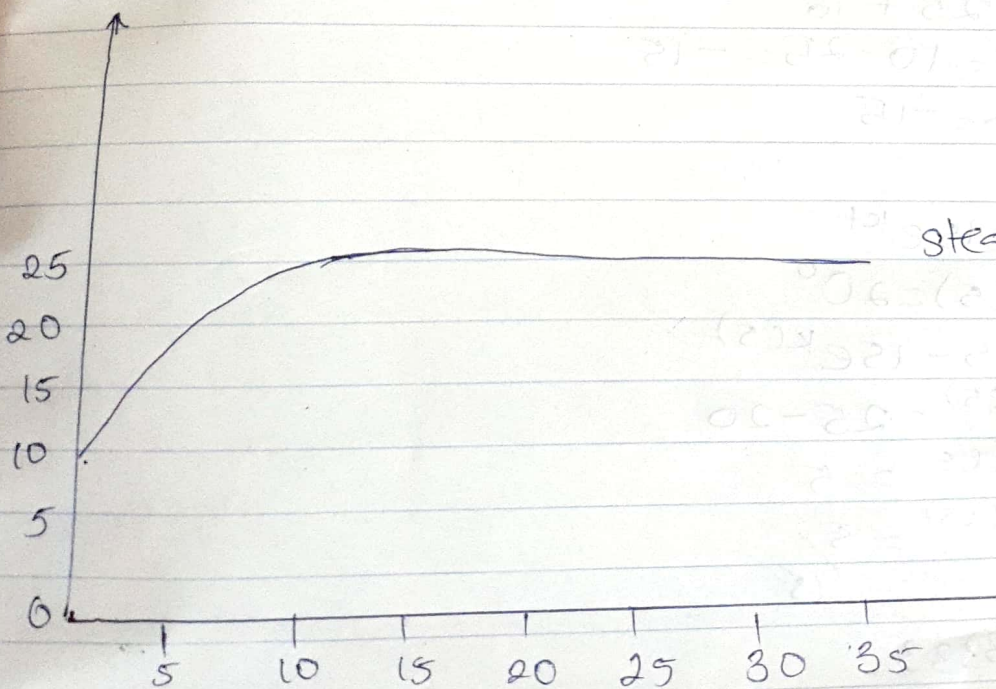
plot(t, y)

grid on

minor grid on

xlabel('Time (secs)')

ylabel('Y axis')



Steady temperature of the system is 25°C
at $t \rightarrow \infty$

$$T = 25 - 15 \cdot \exp(-0.2197 \cdot \infty)$$

$$T = 25^\circ\text{C}$$

(i) Modelling is mathematical representation of a system. It is describing a system using mathematical concepts and language.

ii) Using balance

Differentiation
partial

Using differential equations