

1 (a) Mathematical model is a description of a system using mathematical concepts & language. The process of developing a mathematical model is termed mathematical modelling.

(b) Finite & element analysis

(c) Use of Newton's laws and other laws of physics. the

(c) $\frac{dT}{dt} = K(T - T_s)$ where T = initial temperature of a body
 T_s = surrounding temperatures.

$$\frac{dT}{dt} = K(T - T_s)$$

$$\frac{T - T_s}{T - T_s}$$

$$\ln(T - T_s) = Kt + C$$

$$T - T_s = e^{Kt} \cdot e^C$$

$$\text{let } e^C = C$$

$$\therefore T - T_s = Ce^{Kt}$$

$$\therefore T = T_s + Ce^{Kt}$$

when $t = 0$, $T = 10^\circ\text{C}$ & $T_s = 25^\circ\text{C}$ is a constant

$$10 = 25 + Ce^0$$

$$10 = 25 + C$$

$$C = -15$$

$$T = 25 - 15e^{Kt}$$

when $t = 5\text{mins}$ $T = 20^\circ\text{C}$

$$20 = 25 - 15e^{5K}$$

$$-5 = -15e^{5K}$$

$$e^{5K} = \frac{5}{15}$$

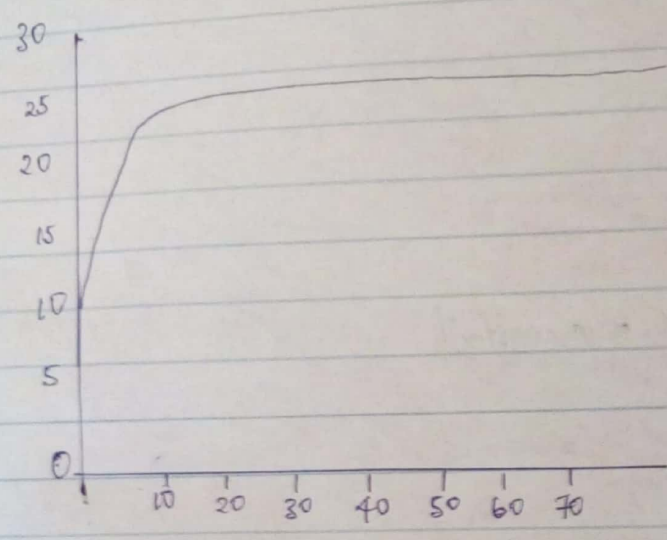
$$5K = \ln\left(\frac{5}{15}\right)$$

$$K = \frac{\ln\left(\frac{5}{15}\right)}{5}$$

$$K = -0.22$$

$$T = 25 - 15e^{-0.22t}$$

(iv)	A	B
1	t	T
2	0	$= 25 - 15 \text{EXP}(-0.22 * A_2)$
3	1	$= 25 - 15 \text{EXP}(-0.22 * A_3)$
4	2	$= 25 - 15 \text{EXP}(-0.22 * A_4)$
5	3	
6	4	
7	5	
8	6	

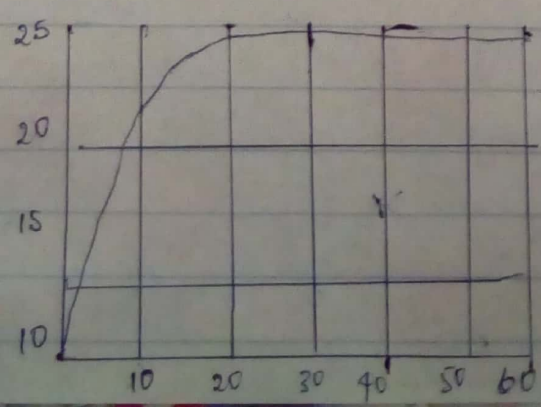


(vi) Command window

```

clear
clc
close all
t = (0:1:60)
T = 25 - 15 * exp(-0.22 * t)
plot (t, T)
grid on
grid minor

```



↔

(ii) The steady state temperature which is the temperature at which the system's temperature stopped increasing is 24.9.

(v) $T = 25 - 15e^{-0.22t}$

when $t \rightarrow \infty$

then $T = 24.9$