

AGUMIR ROSEMARY
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CHEMICAL ENGINEERING
TEST 4

(a) Modelling is the mathematical representation of a system. It is describing the system using mathematical concepts and language.

- (b) Methods of generating a model
- i) Using balance law
 - ii) Using partial differential equation
 - iii) Differentiation

(c) $\frac{dT}{dt} = k(T - T_a)$

$$\int \frac{1}{T - T_a} dT = \int k dt$$

$$\ln(T - T_a) = k + t$$

$$T - T_a = e^{kt+c}$$

$$T - T_a = e^{kt} \cdot e^c$$

$$T - T_a = T_0 e^{kt}$$

when $t = 0$

$$10 = 25 + T_0 e^{k(0)}$$

$$10 = 25 + T_0$$

$$T_0 = 10 - 25 = -15^\circ\text{C}$$

$$T_0 = -15^\circ\text{C}$$

$$T(t) = 25 - 15e^{kt}$$

$$\text{at } t = 5 \text{ min} = 20^\circ$$

$$20 = 25 - 15e^{k(5)}$$

$$15e^{kt} = 5$$

$$e^{kt} = 5/15$$

$$5K = \ln(0.333)$$

$$K = -0.2197$$

$$T(t) = 25 - 15 \exp(-0.2197t)$$

d) Steady temperature of the system is 25°C

e) at $t = 24.9^\circ\text{C}$

$$24.9 = 25 - 15 \exp(-0.2197t)$$

$$-0.1 = -15 \exp(-0.2197t)$$

$$\ln\left(-\frac{0.1}{15}\right) = -0.2197t$$

$$t = 22.8 \text{ secs,}$$

temperature of 8

The system becomes stable at a temperature of 25°C .