

Solⁿ

$$T(a) = 10^\circ\text{C}$$

$$T(0) = 10^\circ\text{C}$$

$$\text{Actual temp} = 25^\circ\text{C} = T_a$$

$$\frac{dT}{dt} = k(T - T_a)$$

$$dT = k(T - T_a) dt$$

$$\frac{dT}{(T - T_a)} = k dt$$

Integrating both sides

$$\ln\left(\frac{T - T_a}{T_0 - T_a}\right) = kL + c$$

$$T - T_a = e^{kL+c}$$

$$\text{Let } e^c \text{ be } A$$

$$T - T_a = A e^{kL}$$

$$T - T_a = A e^{kL}$$

$$T = A e^{kL} + T_a$$

When $T = 10$

$$10 = A e^{k(10)} + 25$$

$$10 = A + 25$$

$$A = 10 - 25$$

$$A = -15$$

$$T_{0.5} = 15 e^{kx}$$

$$T + e^{kx} = 20$$

$$20 = 25 - 15 e^{k(5)}$$

$$20 = 25 - 15 e^{5k}$$

$$15 e^{5k} = 25 - 20$$

$$15 e^{5k} = 5$$

$$e^{5k} = 0.333$$

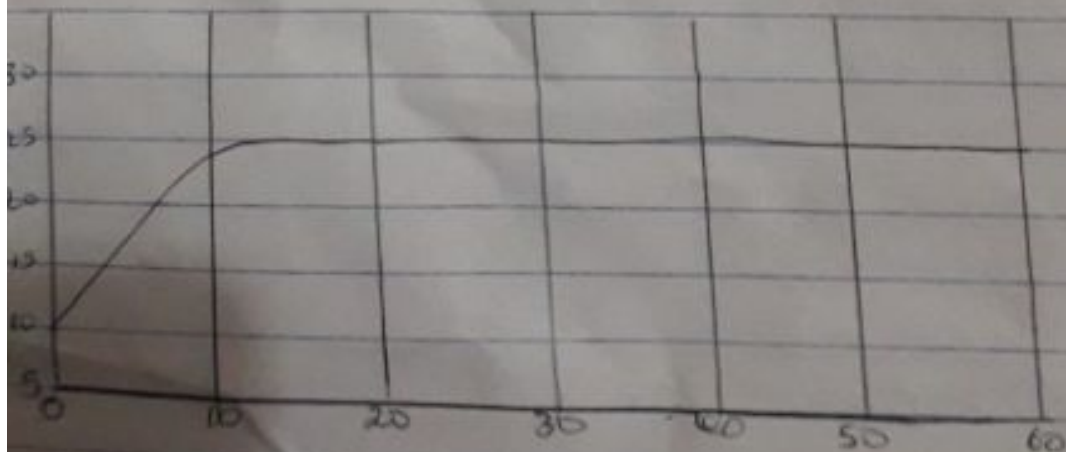
$$5k = 100.333$$

$$5k = -1.0986$$

$$k = 0.22$$

$$T(t) = 25 - 15e^{-0.22t}$$

- Using Microsoft Excel
- Pick a box insert 'f'
- Pick another box insert 't'
- Under the already labelled box 't'
- Insert a value of 0 in an empty box
- Go to fill
- Click on Series
- Insert a step value of 1
- Change the Series into Columns
- Insert a step value of 1
- Change the Series into Columns
- Insert a step value of 60
- Under the already labelled box 'r'
- Pick a box
- Insert " $-25(15)e^{-0.22t}$ "
- Autofill.
- Go to next
- Pick a graph of choice
- Label the graph
- Output



Using Matlab
Command window

clear

cls

Close all

t=0:1:50

t=25-5*4*(1-0.25*t)

Plot (x,T)

grid on

grid minor

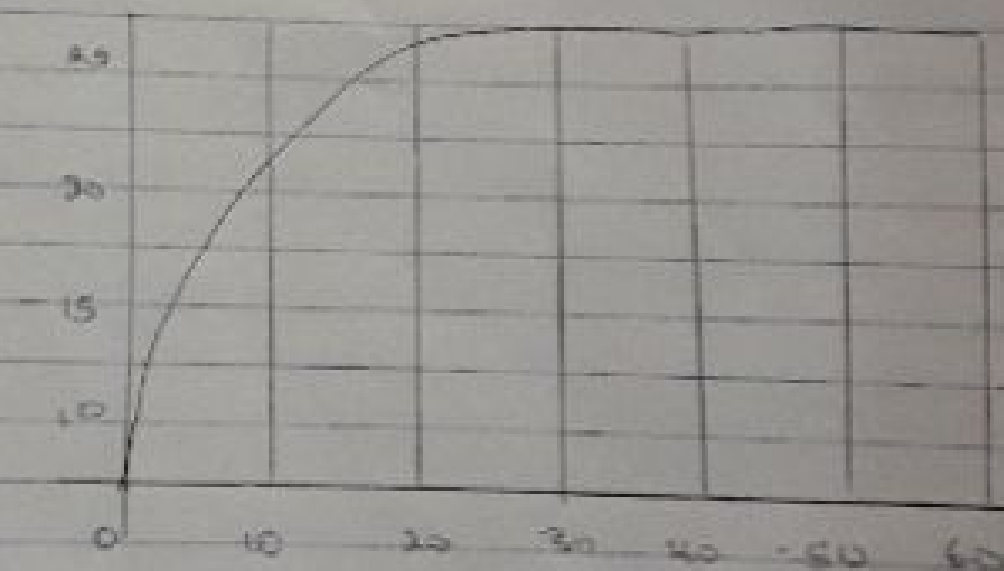
x label ('Time (sec)')

y label ('Temperature')

grid on

grid minor

Output



Using Euler's dynamic response, the state of the system would be 25C at 20 mins.

Using the analytical model equation, the temperature of the thermometer at (0) will be 25°C.