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COLLEGE - ENGINEERING  
DEPARTMENT - MECHANICAL

LEVEL - 200

COURSE - ENG 282

MAT NO - 171ENG061029

a

Mathematical modelling is a mathematical representation of a system and simulation of a system which involves acting the model and obtaining the output variable for different values of its input variable or as input variable is changed from one value to another. -

b

i. Differentiating:

ii

c

$$T(0) = 10^{\circ}\text{C}.$$

$$T(5) = 20^{\circ}\text{C}.$$

$$\text{Actual temp} = 25^{\circ}\text{C} = T_n.$$

$$\frac{\partial T}{\partial t} = k(T - T_n)$$

$$\partial T = k(T - T_n) \partial t$$

$$\frac{\partial T}{(T - T_n)} = k \partial t.$$

Integrating both sides

$$\ln(T - T_n) = kt + c$$

$$T - T_n = e^{kt} + e^c.$$

Let  $e^c$  be A.

$$T - T_n = e^{kt} + A.$$

$$T - T_n = A e^{kt}$$

$$T = A e^{kt} + T_n.$$

$$\text{Insert} = 25 - (15 * \exp[-0.22 * A * t]).$$

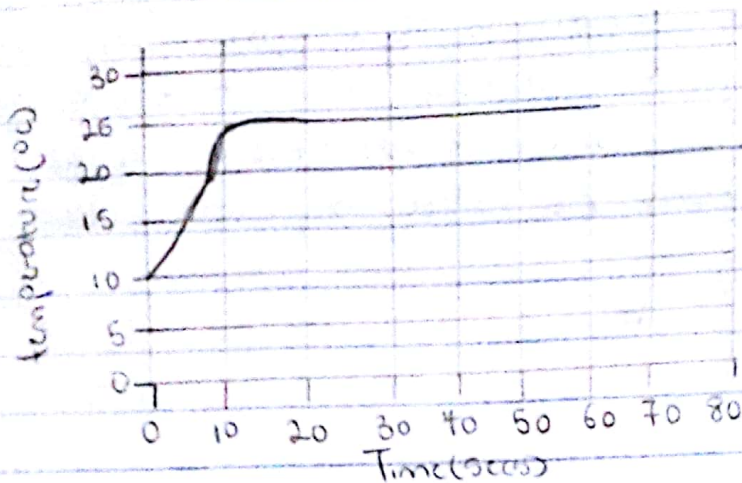
- Auto fill

- Go to insert

Pick a graph of choice.

Label the graph

Output



Using matlab

Command window:

```
clear
```

```
clc
```

```
close all
```

```
t=0:1:60
```

```
T=25-15*exp(-0.22*t)
```

```
Plot(t,T)
```

```
grid on
```

```
grid minor
```

```
xlabel('Time (secs)')
```

```
ylabel('Temperature')
```

```
grid on
```

```
grid minor
```

when  $T=10$ .

$$10 = Ae^{-0.22(10)} + 25$$

$$10 = A + 25$$

$$A = -15$$

$$T = 25 - 15e^{-0.22t}$$



$$A(t) = 20$$

$$20 = 25 - 15e^{-kt}$$

$$20 - 25 = -15e^{-kt}$$

$$15e^{-kt} = 25 - 20$$

$$15e^{-kt} = 5$$

$$e^{-kt} = 0.3333$$

$$kt = \ln 0.3333$$

$$kt = -1.0986$$

$$k = 0.22$$

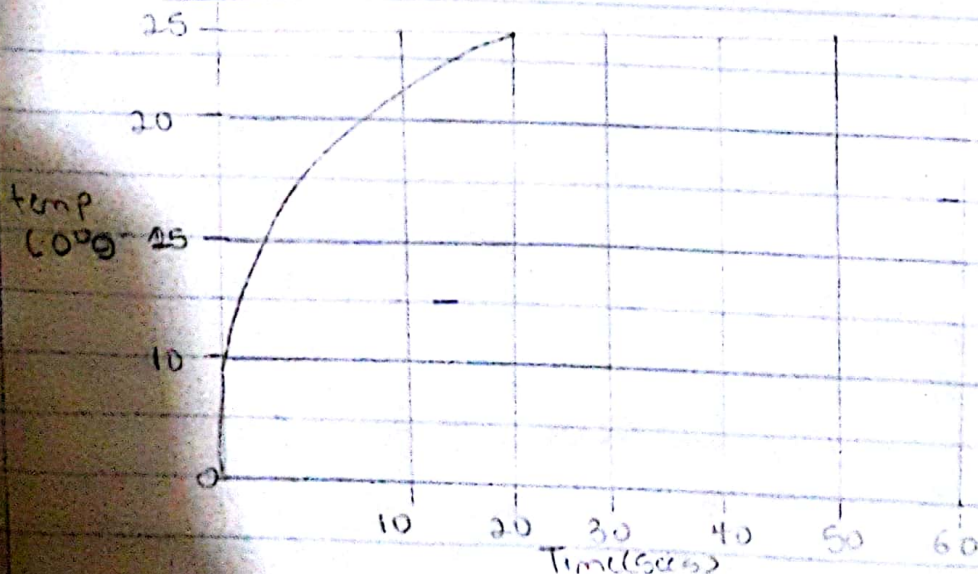
$$T(t) = 25 - 15e^{-0.22t}$$

Relating  
Equation

ii Using Microsoft Excel

- Pick a box insert 't'
- Pick another box insert 'T'
- Undo the already labelled box 't'
- Insert a value of 0 in an empty box.
- Go to fill
- Adjust lock on series.
- Insert a step value of 1
- Change series in to column.
- Insert a stop value of 60.
- Under the already labelled box 2 't'
- Pick a box.

Output



- iv Using excel's dynamic response, the steady state temperature of the system would be  $25^{\circ}\text{C}$  at 20 mins.
- v Using the developed model's equation, the temperature of the thermometer at  $t=0$  will be  $25^{\circ}\text{C}$ .