

NAME HARDING - USOH TITANIA BOLUHARIFE  
MAT NO 18/ENG08/007  
DEPT BIOMEDICAL ENGINEERING  
COURSE ENG 281, ENGINEERING MATHEMATICS I

### ASSIGNMENT 1

1a) Show that the limit of the function given in  $f(x) = \frac{\sin ax}{bx}$  as  $x$  approaches 0 is  $\frac{a}{b}$ .

Solution

$$\lim_{x \rightarrow 0} f(x) = \frac{a}{b}$$

$$\lim_{x \rightarrow 0} \frac{\sin ax}{bx} = \frac{\sin a(0)}{b(0)} = \frac{0}{0}$$

Now Using L'Hospital's rule.

$$\lim_{x \rightarrow 0} \frac{\sin ax}{bx} = \frac{a \cos ax}{b} = \frac{a \cos a(0)}{b} = \frac{a \cos 0}{b}$$

$$= \frac{a(1)}{b} = \frac{a}{b}$$

$$\therefore \lim_{x \rightarrow 0} \frac{\sin ax}{bx} = \frac{a}{b}$$

1b) The Model of a system has been developed to be given in

$$f(x) = 5x - 21$$

Given that  $\delta = 0.1$  and  $\Delta \delta = 0.01$ ,

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 demonstrate in tabular form, that the Limit of  
 the Model as  $x \rightarrow 6$  is equal to 9.

Solution

$$f(x) = 5x - 21$$

$$\lim_{x \rightarrow a} f(x) = L$$

Showing that  $\lim_{x \rightarrow 6} f(x) = 9$

$$\lim_{x \rightarrow 6} (5x - 21) = 9$$

Using

$6 - \delta < x < 6 + \delta$  then  $9 - \epsilon < f(x) < 9 + \epsilon$

where

~~$$\delta = 0.1, \epsilon = 0.5, \delta = 0.01$$~~

for  $\delta$  we start from the (LHS).  $6 - 0.1 = 5.9$

$$6 + 0.1 = 6.1$$

and for  $\epsilon$  we start from the (RHS).  $9 - 0.5 = 8.5$

$$9 + 0.5 = 9.5$$

$x$

$x$	$f(x)$
5.90	8.5
5.91	8.55
5.92	8.60
5.93	8.65
5.94	8.70
5.95	8.75
5.96	8.80
5.97	8.85
5.98	8.90
5.99	8.95
6.00	9.00

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③ Show whether the function given below is continuous on the interval  $[-5, 5]$ .

$$f(x) = (25 - x^2)^{1/2}$$

Solution

~~Substituting~~

$$f(x) = (25 - x^2)^{1/2}$$

when  $x = -5$ .

$$\begin{aligned} f(x) &= (25 - (-5)^2)^{1/2} \\ &= (25 - 25)^{1/2} = \sqrt{0} = 0 \end{aligned}$$

when  $x = -4$

$$\begin{aligned} f(x) &= (25 - (-4)^2)^{1/2} \\ &= (25 - 16)^{1/2} \\ &= \sqrt{9} = 3 \end{aligned}$$

when  $x = -3$

$$\begin{aligned} f(x) &= (25 - (-3)^2)^{1/2} \\ &= (25 - 9)^{1/2} \\ &= \sqrt{16} = 4 \end{aligned}$$

when  $x = -2$

$$\begin{aligned} f(x) &= (25 - (-2)^2)^{1/2} \\ &= (25 - 4)^{1/2} \\ &= 21^{1/2} = \sqrt{21} = 4.58 \end{aligned}$$

when  $x = -1$

$$\begin{aligned} f(x) &= (25 - (-1)^2)^{1/2} \\ &= (25 - 1)^{1/2} \\ &= 24^{1/2} = \sqrt{24} = 2\sqrt{6} \text{ or } 4.899 \end{aligned}$$

when  $x = 0$

$$\begin{aligned} f(x) &= (25 - (0)^2)^{1/2} \\ &= 25^{1/2} = \sqrt{25} = 5 \end{aligned}$$

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when  $x = 1$

$$\begin{aligned} f(x) &= (25 - (1)^2)^{1/2} \\ &= (25 - 1)^{1/2} = 24^{1/2} = \sqrt{24} = 2\sqrt{6} \\ &\approx 4.899 \end{aligned}$$

when  $x = 2$

$$\begin{aligned} f(x) &= (25 - (2)^2)^{1/2} \\ &= (25 - 4)^{1/2} = 21^{1/2} = \sqrt{21} = 4.58 \end{aligned}$$

when  $x = 3$

$$\begin{aligned} f(x) &= (25 - (3)^2)^{1/2} \\ &= (25 - 9)^{1/2} \\ &= \sqrt{16} = 4 \end{aligned}$$

when  $x = 4$

$$\begin{aligned} f(x) &= (25 - (4)^2)^{1/2} \\ &= (25 - 16)^{1/2} \\ &= \sqrt{9} = 3 \end{aligned}$$

when  $x = 5$

$$\begin{aligned} f(x) &= (25 - (5)^2)^{1/2} \\ &= (25 - 25)^{1/2} = 0^{1/2} = \sqrt{0} \\ &= 0 \end{aligned}$$

Comment;  $f(x) = (25 - x^2)^{1/2}$  is continuous on Interval  $[-5, 5]$  because the limit of the function, ~~it~~ <sup>it exists</sup> is defined, and is equal to the value of the function at  $x = [-5, 5]$ .