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COURSE: ENG 281 2002

MAT NO: 18/ENGL04/070

DEPT: ELECT/ELECT.

Show that the limit $x \rightarrow 0$ is $\frac{a}{b}$

$$f(x) = \frac{\sin ax}{bx}$$

putting $x \rightarrow 0$

$$\frac{\sin a(0)}{b(0)} = \text{indefinite}$$

hence applying L'Hopital's

$$\frac{\sin ax}{bx} = \frac{a \cos ax}{b}$$

$$\lim_{x \rightarrow 0}$$

$$\frac{a \cos 0}{b} = \frac{ax}{b} = \frac{a}{b}$$

hence $x \rightarrow 0$ if $f(x) = \frac{a}{b}$

□

b)

$$f(x) = 5x - 21$$

$$\Delta x = 0.1, \quad \Delta y = 0.01$$

$$x \rightarrow 6$$

$$\begin{array}{ccc} | & | & | \\ \hline 5.9 & 6 & 6.1 \end{array}$$

$$\begin{array}{ccc} | & | & | \\ \hline L - \epsilon & L & L + \epsilon \end{array}$$

$L - \Delta$	$a - \Delta$	a	$a + \Delta$	$L + \Delta$
8.50	5.90	6	6.10	9.50
8.55	5.91		6.09	9.45
8.60	5.92		6.08	9.40
8.65	5.93		6.07	9.35
8.70	5.94		6.06	9.30
8.75	5.95		6.05	9.25
8.80	5.96		6.04	9.20
8.85	5.97		6.03	9.15
8.90	5.98		6.02	9.10
8.95	5.99		6.01	9.05
9.00	6.00		6.00	9.00

$[-5, 5]$

$$f(x) = (25 - x^2)^{1/2}$$

when $x = -5$

$$(25 - (-5)^2)^{1/2} \\ = (25 - 25)^{1/2} = 0$$

when $x = -4$

$$(25 - (-4)^2)^{1/2} \\ = (25 - 16)^{1/2} = 3$$

when $x = -3$

$$(25 - (-3)^2)^{1/2} \\ = (25 - 9)^{1/2} = 4$$

when $x = -2$

$$(25 - (-2)^2)^{1/2} \\ = (25 - 4)^{1/2} = 4.58$$

when $x = -1$

$$(25 - (-1)^2)^{1/2} \\ = (25 - 1)^{1/2} = 4.9$$

when $x = 0$

$$(25 - 0)^{1/2} = 5$$

when $x = 1$

$$(25 - (1)^2)^{1/2} = 4.9$$

when $x = 2$

$$(25 - (2)^2)^{1/2} = (25 - 4)^{1/2} \\ = 4.58$$

when $x = 3$

$$(25 - (3)^2)^{1/2} \\ = (25 - 9)^{1/2} = 4$$

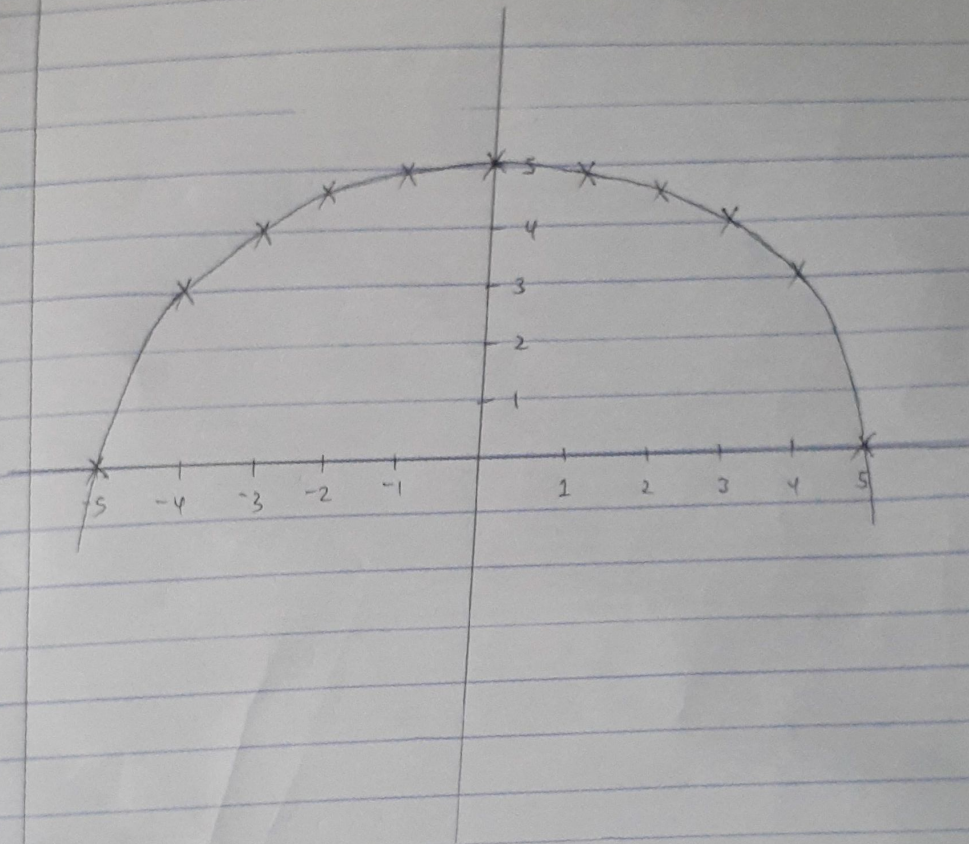
when $x = 4$

$$(25 - (4)^2)^{1/2} = (25 - 16)^{1/2} \\ = 3$$

when $x = 5$

$$(25 - (5)^2)^{1/2} = 0$$

x	-5	-4	-3	-2	-1	0	1	2	3	4	5
$f(x)$	0	3	4	4.58	4.9	5	4.9	4.8	4	3	0



\therefore The function $f(x)$ is continuous.