

8.80	5.96	6.04	9.20
8.85	5.97	6.03	9.15
8.90	5.98	6.02	9.10
8.95	5.99	6.01	9.05
9.00	6.00	6.00	9.00

$$c \quad [-5, 6] \quad f(x) = (25 - x^2)^{1/2}$$

$$\text{at } x = -5$$

$$\text{at } x = 5$$

$$(25 - (-5)^2)^{1/2}$$

$$(25 - 5^2)^{1/2} = 0$$

$$(25 - 25)^{1/2} = 0$$

$$\text{at } x = -4$$

$$\text{at } x = 4$$

$$(25 - (-4)^2)^{1/2}$$

$$(25 - 4^2)^{1/2} = 3$$

$$(25 - 16)^{1/2} = 3$$

$$\text{at } x = 3$$

$$\text{At } x = -3$$

$$(25 - 3^2)^{1/2} = 4$$

$$(25 - (-3)^2)^{1/2}$$

$$\text{at } x = 2$$

$$(25 - 9)^{1/2} = 4$$

$$(25 - 2^2) = 21.58$$

$$\text{At } x = -1$$

$$\text{at } x = 1$$

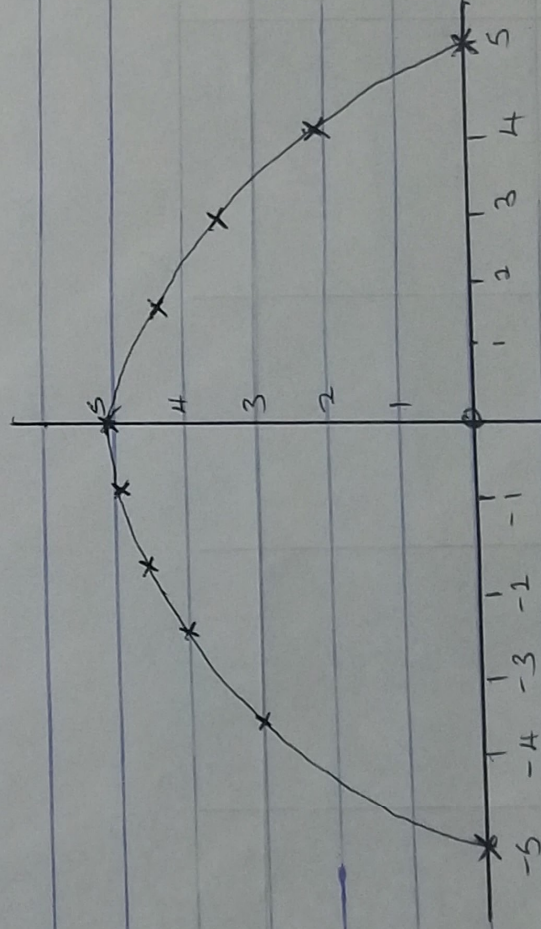
$$(25 - (-1)^2)^{1/2}$$

$$(25 - 1^2)^{1/2} = 4.9$$

$$(25 - 1)^{1/2} = 4.9$$

$$\text{At } x = 0$$

$$(25 - 0^2)^{1/2} = 5$$



Hence, the eqn $f(x) = (25 - x^2)^{1/2}$ is Continuous

- 1) Show that the limit of the function given in equation (1.1) as x approaches 0 is a/b

$$f(x) = \frac{\sin ax}{bx}$$

Solution

$$f(x) = \frac{\sin ax}{bx}$$

$$\lim_{x \rightarrow 0} \frac{\sin ax}{bx} = \frac{\sin ax}{bx}$$

$$f(x) = \frac{\sin a(0)}{b(0)} = \frac{0}{0} \quad \therefore \text{(Undefined)}$$

Using L'Hopital's rule

$$f(x) = \frac{\sin ax}{bx}$$

$$f(x) = \frac{a \cos ax}{b} = \frac{a \cos a(0)}{b} = \frac{a}{b}$$

- 2 The model of a System has been developed to be as given in equation (1.2). $F(x) = 5x - 2$. Given that $\delta = 0.1$ and $\Delta \delta = 0.01$, determine in a tabular form that the limit of the model as $x \rightarrow 6$ is equal to 9

Soln

$$f(x) = 5x - 2 \quad \delta = 0.1, \quad \Delta \delta = 0.01, \quad a = 6$$

L-e	$a - \delta$	a	$a + \delta$	L+e
8.5	5.9	6	6.1	9.5
8.55	5.91		6.09	9.45
8.6	5.92		6.08	9.4
8.65	5.93		6.07	9.35
8.7	5.94		6.06	9.3
8.75	5.95		6.05	9.25