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1812ng031010

Electrical engineering

a) $\lim_{x \rightarrow 0} f(x) = \frac{a}{b}$ for $f(x) = \frac{\sin ax}{bx}$

By direct substitution

$\lim_{x \rightarrow 0} \frac{\sin ax}{bx} = \frac{\sin(a \cdot 0)}{b \cdot 0} = \frac{0}{0} = \text{undefined}$

Apply L'Hopital's rule and substitute

$\lim_{x \rightarrow 0} \frac{\sin ax}{bx} = \frac{a \cos ax}{b}$

$\lim_{x \rightarrow 0} = \frac{a \cos a \cdot 0}{b} = \frac{a}{b} = \left(\cos 0 = 1 \right)$

$\frac{\sin ax}{bx} = \frac{a}{b}$

b) $f(x) = 5x - 21$

$\Delta = 0.1 \quad \Delta x = 0.01$

let x_2 and x_1 be values of x such that

$x_2 - x_1 = \Delta = 0.1$, then $f(x_2) - f(x_1) = \Delta$

$\Delta = 5x_2 - 21 - [5x_1 - 21]$

$\Delta = 5x_2 - 5x_1 - 21 + 21$

$\Delta = 5(x_2 - x_1)$

$\Delta = 5 \times \Delta$

$\Delta = 5 \times 0.1$

$= 0.5 = 5 \times \Delta \Rightarrow \Delta = 5 \times 0.01 = 0.05$

x	f(x)
5.9	8.5
5.91	8.55
5.92	8.60
5.93	8.65
5.94	8.70
5.95	8.75
5.96	8.80
5.97	8.85
5.98	8.90
5.99	8.95

x	f(x)
6.1	9.5
6.09	9.45
6.08	9.40
6.07	9.35
6.06	9.30
6.05	9.25
6.04	9.20
6.03	9.15
6.02	9.10
6.01	9.05