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Biomedical Engineering

17/ENG08/004

ENG 381 ASSIGNMENT II

ENGINEERING MATHEMATICS III

QUESTION 1.

$$y = e^{x^2+x}$$

$$\text{let } u = x^2+x \quad \frac{dy}{dx} = 2x+1$$

$$y = e^u \quad \frac{dy}{du} = e^u$$

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} = e^u (2x+1)$$

$$(2x+1)e^{x^2+x}$$

$$\frac{d^2y}{dx^2} = u = (2x+1)$$

$$v = e^{x^2+x}$$

$$\frac{dy}{dx} = 2$$

$$\frac{dy}{dx} = (2x+1)e^{x^2+x}$$

$$(2x+1)(2x+1)e^{x^2+x} + 2e^{x^2+x}$$

$$\frac{d^2 y}{dx^2} = y'(2x+1) + 2y$$

$$-y'' = -y'(2x+1) + 2y$$

$$A = B + C.$$

$$A = -y'' \quad x^n = -y^{2+n}$$

$$B = y'(2x+1)$$

$$u = y' \quad y^n = -y^{1+n}$$

$$v = 2x+1 \quad v' = 2$$

$$B^n = -y^{1+n}(2x+1) + 2ny^n + 0$$

$$C = 2y$$

$$u = 2y^{\frac{1}{2}} = 2y^n$$

$$\therefore -y^{2+n} = y^{1+n}(2x+1) + 2ny^n + 2y^n$$

$$y^{2+n} = (2x+1)y^{1+n} + 2y^n(n+1)$$

## QUESTION 2.

i.  $y = x^3 e^{4x}$

$$u = e^{4x}; \quad u' = 4e^{4x}; \quad u'' = 16e^{4x}; \quad u''' = 64e^{4x}$$

$$u^{(4)} = 256e^{4x}; \quad u^{(5)} = 1024e^{4x}$$

$$v = x^3; \quad v' = 3x^2; \quad v'' = 6x; \quad v''' = 6; \quad v^{(4)} = 0; \quad v^{(5)} = 0$$

Using Leibnitz theorem

$$y^{(5)} = u^{(5)}v + 5u^{(4)}v' + \frac{5(5-1)}{2!}u^{(3)}v'' + \frac{5(5-1)(5-2)}{3!}u^{(2)}v''' + \dots$$

$$y^{(5)} = 1024e^{4x}x^3 + 5(256e^{4x})(3x^2) + \frac{5(5-1)}{2!}64e^{4x}(6) + \dots$$

$$\frac{5(5-1)(5-2)}{3} 16e^{4x}(6) + \frac{5(5-1)(5-2)(5-3)}{2!} 4e^{4x}(6) + 0$$

$$= 1024x^3 e^{4x} + 3840x^2 e^{4x} + \frac{20}{2!} 384x e^{4x} + \frac{60}{3!} 96e^{4x}$$

+ 0

$$y^5 = 1024x^3 e^{4x} + 3840x^2 e^{4x} + 3840x e^{4x} + 960e^{4x} + 0$$

$$y^5 = 4e^{4x} (256x^3 + 960x^2 + 960x + 240)$$

$$4e^{4x} \cdot 16 (16x^3 + 60x^2 + 60x + 15)$$

$$y^5 = 64e^{4x} (16x^3 + 60x^2 + 60x + 15)$$

ii  $x^2 \frac{d^2 y}{dx^2} + x \frac{dy}{dx} + y = 0$

$$x^2 y'' + x y' + y$$

$$A + B + C = 0$$

$$A = x^2 y''$$

$$u = y^{2+n} \quad u' = y^{2+n}$$

$$v' = x^2 \quad v' = 2x; \quad v'' = 2$$

$$x^n = y^{2+n} x^2 + n 2x y^{1+n} + \frac{n(n-1)}{2} 2 y^n + 0$$

$$x^n = x^2 y^{2+n} + 2n x y^{1+n} + (n^2 - 1) y^n + 0$$

$$B = x y'$$

$$u = y^1 \quad u' = y^{1+n}$$

$$v = x \quad v' = 1 \quad v'' = 0$$

