Chianeke Okwudili 17/eng01/006 Chemical engineering Quexion 1 Defenerthing 1: e" let 4 = 22+2 dydaz 2x+1 M/du = eu Signestiating ling Function of Function

1y = dy x dy = All (2xt) = (2xt) ext + x

dx dy dx Differentiating viens function of function dv/dz x dv/dz x dz/dz let Z = x2+x dz/dx = 2xt1  $dv/dz = e^{z} = e^{x^{2}tx}$   $dv = e^{x}(2xt1) = e^{(x^{2}tx)}(2xt1)$ dx dv = (2x+) extx. Differentiating Voing Product Rule = 4 1/42 + V dy/dz

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dry = (2x+1) [(2x+1) ex+x] + e(x2+x) + 2
 dy = (2211) ((2211) (22) +2 (242)
 But Y= extx & Y' = (2xt) extx

d'y = Y'(2xt) + 2Y.
 Since dey . Y"
Y" = Y'(2xt) + 24
 1'(2xt1) + 24-7" = D
let 4, = 1' (ext)
  Kl2: 24
 M3 = /11.
For W.
                            for 1/2
7 2 7' , V = 2x+1
                           V = V^n V = 0 V' = 0
U(0-) = V(0) V"=0
For Kla
11" 2 Y (DAZ) V20
y (n-1) , y cn+1)
Lecell.
Y"= U"V+ ny(n-1) V'+ n(n-1) U(n-2) V2+ n(n-1)(n-2) U(n-3) V3+
Y (n+2) = (2x+1) y(n+1) + 2(n+1)yn.
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Question 2 y = 2 2 2 42 f n(n-1)(n-2)(n-3)(n-4) (n-5) ys + - - -- $\frac{1}{1} = e^{4x} \qquad V = x^{3}$   $\frac{1}{1} = e^{4x} \qquad V^{(1)} = 3x^{2}$ 11(n-1)=4(n-1)=4x V(a)=6x ((m=2) 4(m=2) 64x V(3) = 6 U(n-3) 4 (n-3) e +x V(4) = O  $1^{n} = 4^{n}e^{4x} \cdot x^{3} + n4^{(n-1)}e^{4x} \cdot 3x^{2} + n(n-1) + 4^{(n-2)}e^{4x} \cdot 6x + n(n-1)(n-2) + 4^{(n-3)}e^{4x} \cdot 6x + n(n-1)(n-2) + 4^{(n-3)}e^{4x}$ y(5) = 4(5) 4x 3+ 5[4(5-1) e4x, 3x2] + 5(5-1) 4(5-2) 42.6x + 5(5-1)(5-2) 4(5-3) 42.6  $40^{2} + 54^{(5)} + 54^{(4)} + 54^{(4)} + 54^{(4)} + 54^{(4)} + 54^{(4)} + 54^{(2)} +$ 2! 31. YET, 1024 x<sup>2</sup>e<sup>4x</sup> + 3840 x<sup>2</sup>e<sup>4x</sup> + 7680 xce<sup>4x</sup> + 5760 e<sup>4x</sup> 15= 1024 x3e+x+ 384022e+x+ 3840xe+x + 960e+x 45. etx [1024x3+3840x2+3840x +960]. Question 3. x2 d2y + xdy + y = 0. x2 y" + x Y' + y =0 Ky = 22 4" 142 2 x y' 143 = 1.

$A = \chi^2 \chi''$
1 = 1 <sup>2</sup> V = 1 <sup>2</sup>
7/n= 1(n+2) 1/2 2x
$\int \sqrt{(n-1)^2} \sqrt{(n+1)} \qquad \sqrt{2} = 2$
$V^{(n-2)} = V^{n} \qquad V^{3} = 0$
W2 2 X1'
Mz Y' Vz X
2/n = /(n+1) V'21
V (n-1) = V220
123 = 1
1/" z \" \" z 0
> It for Lectority theorem.
$U^{(n)}V + nU^{(n-1)}V^{1} + n(n-1)U^{(n-2)}V^{2} + n(n-1)(n-2)U^{(n-3)}V^{(3)} +$
2! 3!
$= \sqrt{\frac{(n+2)}{2}} + n(\sqrt{\frac{(n+2)}{2}} + n(n-1) \sqrt{\frac{2}{2}} + n(n-1)$
8! 3!
$= \sum_{n=1}^{\infty} \frac{1}{2} + n y^{(n+1)} 2x + n (n-1) y^{n} + 2 + y^{(n+1)} x + n y^{n} + 1 + y^{n} + 2 = 0$
2
72 (n+2) + 2 m (mt) + (01) 2 1/1 + 2 (n+1) , 2/1 + 1/1 0
$\frac{x^{2}\sqrt{n+2}}{+2\pi n\sqrt{mn}} + \frac{n(n-1)}{2}\sqrt{n} + \frac{2}{\pi\sqrt{n+1}} + \frac{n}{2}\sqrt{n} + \frac{1}{2}\sqrt{n}$
$x^{2}y^{(n+2)} + 2xny^{(n+1)} + n(n-1)y^{n} + xy^{(n+1)} + ny^{(n)} + xy^{(n+1)} = 0$
$\frac{2}{2} \cdot (nt^2) \qquad (nt) \qquad (nt)$
$x^{2}y^{(n+2)} + 2xny^{(n+1)} + xy^{(n+1)} + n(n-1)y^{n} + ny^{n} + y^{n} = 0$
$x^{2}y^{(n+2)}+(2n+1)x^{(n+1)}+[n(n-1)+n+1]y^{n}=0$ .
$x^{2}y^{(n+2)} + (2n+1)xy^{(n+1)} + (n^{2}+1)y^{(n)} = 0$

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