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$$5x^2 + y^2 = 5$$

$$x^2 + y^2 = 4$$

Solve it Simultaneously

$$1 \times 5x^2 + y^2 = 5$$

$$1 \times x^2 + y^2 = 4$$

$$5x^2 + y^2 = 5$$

$$- x^2 + y^2 = 4$$

$$4x^2 = 1$$

$$\frac{4x^2}{4} = \frac{1}{4}$$

$$x^2 = \frac{1}{4}$$

$$4$$

$$x = \sqrt{1/4} = 1/2$$

Substitute $x = 1/2$ in equation ①

$$(1/2)^2 + y^2 = 4$$

$$1/4 + y^2 = 4$$

$$y^2 = 4 - 1/4$$

$$y^2 = 3 3/4$$

$$y = \sqrt{3 3/4}$$

$$= \sqrt{15}/2$$

$$\tan \theta = dy/dx$$

Differentiate Equation ①

$$5x^2 + y^2 = 5$$

$$10x + 2y \frac{dy}{dx} = 0$$

$$\frac{2y \frac{dy}{dx}}{2y} = \frac{-10x}{2y}$$

$$2y$$

$$= \frac{-5x}{y}$$

$$y$$

Substitute $x = 1/2$ and $y = \sqrt{15}/2$

$$\frac{dy}{dx} = \frac{-5(1/2)}{\sqrt{15}/2}$$

$$\sqrt{15}/2$$

$$= 1.291$$

$$\tan \theta_1 = dy/dx$$

$$\theta_1 = \tan^{-1} dy/dx$$

$$\theta_1 = \tan^{-1}(-1.291)$$

$$= -52.239$$

Differentiate eqn. ②

$$x^2 + y^2 = 4$$

$$2x + 2y \frac{dy}{dx} = 0$$

$$\frac{2y \frac{dy}{dx}}{2y} = \frac{-2x}{2y}$$

$$2y$$

$$2y$$

$$\frac{dy}{dx} = \frac{-x}{y}$$

$$= \frac{-1/2}{\sqrt{15}/2} = -0.258$$

$$\sqrt{15}/2$$

$$\frac{dy}{dx} \tan \theta_2 = \frac{dy}{dx}$$

$$\theta_2 = \tan^{-1} \frac{dy}{dx} = -14.775$$

$$\theta_2 - \theta_1 = -52.239 - (-14.775)$$

$$= -52.239 + 14.775$$

$$= -37.4615$$

$$|\theta_2 - \theta_1| = 37.4615$$

$$\approx 37.46^\circ$$

$$-0.5$$

$$1.936$$

$$g(x) := \sqrt{4 - x^2}$$

$$f(x) := \sqrt{5 - 5x^2}$$

