

$$5x^2 + y^2 = 5 \quad \text{--- (i)}$$

$$x^2 + y^2 = 4 \quad \text{--- (ii)}$$

$$y^2 = 5(1 - x^2) \quad \text{--- (i)}$$

sub. for  $y^2$  in eqn. (ii)

$$x^2 + (5(1 - x^2)) = 4$$

$$-x^2 + 5 - 5x^2 = 4$$

$$x^2 - 5x^2 = 4 - 5$$

$$\frac{-4x^2}{-4} = \frac{-1}{-4}$$

$$x^2 = \frac{1}{4} \Rightarrow$$

$$x = \sqrt{\frac{1}{4}} = \frac{1}{2}$$

$$5x^2 + y^2 = 5$$

Differentiate using implicit differentiation

$$10x + 2y \frac{dy}{dx} = 0$$

$$10x + 2y \frac{dy}{dx} = 0$$

$$\frac{2y}{2y} \frac{dy}{dx} = \frac{-10x}{2y}$$

$$\frac{dy}{dx} = \frac{-10(\sqrt{\frac{1}{4}})}{2(\sqrt{\frac{15}{4}})}$$

$$\frac{dy}{dx} = \frac{-5}{\sqrt{15}}$$

$$\frac{dy}{dx} = \tan \theta$$

$$\theta = \tan^{-1} \frac{-5}{\sqrt{15}} \quad \theta = -52.29$$

Using method: Point of Intersection:

$$(-0.5, 1.94) \quad (0.5, 1.93)$$

Substituting  $x$  in eqn (ii)

$$\left(\sqrt{\frac{1}{4}}\right)^2 + y^2 = 4$$

$$\frac{1}{4} + y^2 = 4$$

$$y^2 = 4 - \frac{1}{4}$$

$$y^2 = \frac{16 - 1}{4} = \frac{15}{4}$$

$$y = \sqrt{\frac{15}{4}} \Rightarrow 1.9365$$

$$y = \frac{\sqrt{15}}{2} = 1.9365$$

$$x^2 + y^2 = 4 \dots$$

$$\frac{dy}{dx} = 2x + 2y \frac{dy}{dx} = 0$$

$$\frac{dy}{dx} = \frac{-2x}{2y}$$

$$\frac{dy}{dx} = \frac{-2(\frac{1}{2})}{2(\frac{\sqrt{15}}{2})}$$

$$\frac{dy}{dx} = \frac{-1}{\sqrt{15}}$$

$$\frac{dy}{dx} = \tan \theta$$

$$\theta = \tan^{-1} \left( \frac{-1}{\sqrt{15}} \right)$$

$$\theta = -14.48$$

