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Matric #: 18 (ENAO71011)

Solution to Assignment

$$5x^2 + y^2 = 5 \quad \text{--- (1)} \Rightarrow y^2 = 5 - 5x^2$$

$$x^2 + y^2 = 4 \quad \text{--- (2)}$$

$$y = \sqrt{5 - 5x^2}$$

$$y^2 = 4 - x^2$$

$$f(x) = \sqrt{5 - 5x^2}$$

Let $y = 4 - x^2$ into eq (1)

$$5x^2 + 4 - x^2 = 5$$

$$4x^2 + 4 - 5 = 0$$

$$4x^2 - 1 = 0$$

$$4x^2 = 1$$

$$x^2 = \frac{1}{4}$$

$$x = \pm \frac{1}{2}$$

$$y^2 = 4 - x^2$$

$$y = \sqrt{4 - x^2}$$

$$g(x) = \sqrt{4 - x^2}$$

Using $x = \pm \frac{1}{2}$ (Using Positive first then Negative)

$$\left(\frac{1}{2}\right)^2 + y^2 = 4$$

$$\frac{1}{4} + y^2 = 4$$

$$y^2 = 4 - \frac{1}{4}$$

$$y^2 = 3.75$$

$$y = \pm 1.936$$

$$\frac{dy}{dx} = 5x^2 + y^2 = 5$$

$$10x + 2y \frac{dy}{dx} = 0$$

$$2y \frac{dy}{dx} = -10x$$

$$\frac{dy}{dx} = \frac{-10x}{2y} = \frac{-5x}{y}$$

$$x = 0.5$$

$$\tan^{-1} = 1.2913 = -52.25^\circ$$

$$\frac{dy}{dx} = x^2 + y^2 = 4$$

$$2x + 2y \frac{dy}{dx} = 0$$

$$2y \frac{dy}{dx} = -2x$$

$$\frac{dy}{dx} = \frac{-2x}{2y} = \frac{-x}{y} = \frac{-0.5}{1.936}$$

$$= -0.2583$$

$$\tan^{-1}(-0.2583) = -14.48$$

\therefore the total angle

$$\theta_2 - \theta_1 = -14.48 - (-52.25)$$

$$= 37.77^\circ$$

$$= 38.01$$

