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CHEMICAL ENGINEERING
KINETUG 281

$y^2 = 5(1-x^2)$... (i) using point of intersection $(0.5, 1.97)$, $(0.5, 1.93)$.

$$x^2 + y^2 = 4 \dots (ii)$$

$$y^2 = 5(1-x^2) \dots (i)$$

Substitute for y^2 in eqn (ii)

$$x^2 + 5(1-x^2) = 4$$

$$x^2 + 5 - 5x^2 = 4$$

$$-4x^2 = 4 - 5$$

$$-4x^2 = -1$$

$$x^2 = \frac{-1}{-4} = \frac{1}{4}$$

$$x = \sqrt{\frac{1}{4}} = \frac{1}{2}$$

$$5x^2 + y^2 = 5$$

differentiating implicitly

$$10x + 2y \frac{dy}{dx} = 0$$

$$2y \frac{dy}{dx} = -10x$$

$$\frac{dy}{dx} = \frac{-10x}{2y}$$

$$y^2 = \frac{5(1-x^2)}{\sqrt{15}x}$$

$$x = \frac{1}{2} \text{ and } y = \frac{\sqrt{15}}{2}$$

$$\frac{dy}{dx} = \frac{-10(\frac{1}{2})}{2(\frac{\sqrt{15}}{2})}$$

$$\frac{dy}{dx} = \frac{-5}{\sqrt{15}}$$

$$\frac{dy}{dx} = \tan \theta$$

$$\theta = \tan^{-1} \left(\frac{-5}{\sqrt{15}} \right) = -52.24^\circ$$

Substituting x in eqn (i)

$$\left(\frac{1}{2}\right)^2 + y^2 = 4$$

$$\frac{1}{4} + y^2 = 4$$

$$y^2 = 4 - \frac{1}{4}$$

$$y = \sqrt{4 - \frac{1}{4}} = \frac{\sqrt{15}}{2} = 1.9365$$

