

Substitute x in eqn (i)

$$(\sqrt{1/4})^2 + y^2 = 4$$

$$1/4 + y^2 = 4$$

$$y^2 = 4 - 1/4$$

$$y^2 = \frac{16-1}{4} = y = \sqrt{\frac{15}{4}} = 1.9365$$

$$x^2 + y^2 = 4$$

(differentiate)

$$2x + 2y \frac{dy}{dx} = 0$$

$$\frac{dy}{dx} = -\frac{2x}{2y}$$

$$= -\frac{2(1/2)}{2(\sqrt{15})}$$

$$\frac{dy}{dx} = \frac{-1}{\sqrt{15}}$$

$$\frac{dy}{dx} = \tan \theta$$

$$\theta_2 = \tan^{-1} \left(\frac{-1}{\sqrt{15}} \right)$$

$$\theta_2 = -14.48$$

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$$x^2 + y^2 = 4 \dots (i)$$

$$5x^2 + y^2 = 4 \dots (ii)$$

solution

$$y^2 = 5(4 - x^2) \dots (iii)$$

substitute for y^2 in eqn (i)

$$x^2 + 5(4 - x^2) = 4$$

$$x^2 + 20 - 5x^2 = 4$$

$$x^2 - 5x^2 = -1$$

$$-4x^2 = -1$$

$$x^2 = \frac{-1}{-4}$$

$$x^2 = \frac{1}{4}$$

$$x = \sqrt{\frac{1}{4}}$$

$$x = \frac{1}{2}$$

substitute $x = \frac{1}{2}$ into eqn (i)

$$\left(\frac{1}{2}\right)^2 + y^2 = 4$$

$$\frac{1}{4} + y^2 = 4$$

$$y^2 = 4 - \frac{1}{4}$$

$$y^2 = \frac{15}{4}$$

$$y = \sqrt{\frac{15}{4}}$$

$$5x^2 + y^2 = 5$$

differentiate using implicit differentiation

$$10x + 2y \frac{dy}{dx} = 0$$

$$10x + 2y \frac{dy}{dx} =$$

$$\frac{2y \frac{dy}{dx}}{2y} = \frac{-10x}{2y}$$

$$\frac{dy}{dx} = \frac{-10\left(\frac{1}{2}\right)}{2\left(\sqrt{\frac{15}{4}}\right)}$$

$$\frac{dy}{dx} = \frac{-5}{\sqrt{15}}$$

$$\frac{dy}{dx} = \tan \theta$$

$$\theta = \tan^{-1} \frac{-5}{\sqrt{15}}$$

$$\theta = -52.024$$

