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$$x^2 + y^2 = 4 \dots (i)$$

$$5x^2 + y^2 = 4 \dots (ii)$$

Solution

$$y^2 = 5(1-x^2) \dots (iii)$$

Substitute for y^2 in eqn (i)

$$x^2 + 5(1-x^2) = 4$$

$$x^2 + 5 - 5x^2 = 4$$

$$x^2 - 5x^2 = -1$$

$$-4x^2 = -1$$

$$x^2 = \frac{-1}{-4}$$

$$x^2 = \frac{1}{4}$$

$$x = \sqrt{\frac{1}{4}}$$

$$x = \frac{1}{2}$$

Substitute $x = \frac{1}{2}$ into eqn (i)

$$\left(\frac{1}{2}\right)^2 + y^2 = 4$$

$$\frac{1}{4} + y^2 = 4$$

$$y^2 = 4 - \frac{1}{4}$$

$$y^2 = \frac{15}{4}$$

$$y = \sqrt{\frac{15}{4}}$$

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$$x^2 + y^2 = 4$$

(differentiate)

$$2x + 2y \frac{dy}{dx} = 0$$

$$\frac{dy}{dx} = \frac{-2x}{2y}$$

$$= \frac{-2(\frac{1}{2})}{2(\sqrt{15})}$$

$$\frac{dy}{dx} = \frac{-1}{\sqrt{15}}$$

$$\frac{dy}{dx} = \tan \theta$$

$$\theta = \tan^{-1} \left(\frac{-1}{\sqrt{15}} \right)$$

$$\theta = -14.48$$

(2)

$$5x^2 + y^2 = 5$$

Differentiate Using Implicit differentiation

$$10x + 2y \frac{dy}{dx} = 0$$

$$10x + 2y \frac{dy}{dx} =$$

$$\frac{2y}{2y} \frac{dy}{dx} = \frac{-10x}{2y}$$

$$\frac{dy}{dx} = \frac{-10(\frac{1}{2})}{2(\frac{\sqrt{15}}{4})}$$

$$\frac{dy}{dx} = \frac{-5}{\sqrt{15}}$$

$$\frac{dy}{dx} = \tan \theta$$

$$\theta = \tan^{-1} \frac{-5}{\sqrt{15}}$$

$$\theta = -52.24$$

Substitute x in eqn(ii)

$$\left(\frac{\sqrt{15}}{4}\right)^2 + y^2 = 4$$

$$\frac{15}{16} + y^2 = 4$$

$$y^2 = 4 - \frac{15}{16}$$

$$y^2 = \frac{16-15}{4} = y = \sqrt{\frac{15}{4}} = 1.9365$$

