

$$1) 5x^2 + y^2 = 5$$

$$x^2 + y^2 = 4$$

Solution

$$y^2 = 5x^2 - 5 \dots (i)$$

$$x^2 + y^2 = 4 \dots (ii)$$

Substitute y^2 (i) into eqn

$$x^2 + (5x^2 - 5) = 4$$

$$6x^2 - 5x^2 + 5 = 4$$

$$-4x^2 + 5 - 4 = 0$$

$$-4x^2 + 1 = 0$$

Multiply both sides by -1

$$4x^2 - 1 = 0$$

$$x = +0.5, -0.5$$

Sub x in equation (i)

$$y^2 = 5 - 5(0.5)^2$$

$$y = \sqrt{15}/2$$

Differentiating $5x^2 + y^2 = 5$

$$\Rightarrow 10x + 2y \frac{dy}{dx} = 0$$

$$\frac{dy}{dx} = \frac{-10x}{2y} = \frac{-5x}{y}$$

Differentiating $x^2 + y^2 = 4$

$$\Rightarrow 2x + 2y \frac{dy}{dx} = 0$$

$$\frac{dy}{dx} = \frac{-2x}{2y} = \frac{-x}{y}$$

At $x = 0.5, y =$

$$-5x/y = \frac{-5(0.5)}{\sqrt{15}/2} = \frac{-\sqrt{15}}{2}$$

$$\text{at } x = -\frac{1}{2}, y = \frac{\sqrt{15}}{2}$$

$$-5x/y = \frac{5/2}{\sqrt{15}/2} = \frac{\sqrt{15}}{3}$$

$$\text{at } x = 1/2, y = \sqrt{15}/2 \rightarrow \frac{dy}{dx} = \frac{0.5}{\sqrt{15}/2} = \frac{\sqrt{15}}{15}$$

$$\text{at } x = -1/2, y = \sqrt{15}/2 = x/y = \frac{-1/2}{\sqrt{15}/2} = \frac{-\sqrt{15}}{15}$$

$$\tan(\theta_2 - \theta_1) = \frac{m_2 - m_1}{1 + m_2 m_1}$$

$$\text{When } m_2 = \frac{\sqrt{15}}{3}, m_1 = +\frac{\sqrt{15}}{3}$$

$$\tan(\theta_2 - \theta_1) = \frac{\frac{\sqrt{15}}{10} - \frac{\sqrt{15}}{10}}{0 + (\frac{\sqrt{15}}{10})(\frac{\sqrt{15}}{10})}$$

$$\tan^{-1}(\frac{\sqrt{15}}{5}) = -39.712$$

$$\text{The angle between them } 180 - 39.76 = 140.24^\circ$$

$$f(x) := \sqrt{5 - 5x^2}$$

$$g(x) := \sqrt{4 - x^2}$$

