

① Find the area bounded by the curves $y = 3e^{2x}$ and $y = 3e^{-x}$ and the ordinates at $x=1$ and $x=2$

Solution

① $y_1 = 3e^{2x}$ and $y_2 = 3e^{-x}$
 $x=1$ and $x=2$

$$dA = (y_1 - y_2) dx$$
$$\int_1^2 (3e^{2x} - 3e^{-x}) dx$$

Integral

$$3e^{2x} = \frac{3e^{2x}}{2}$$

$$3e^{-x} = -3e^{-x}$$

$$\int_1^2 \frac{3e^{2x}}{2} + 3e^{-x}$$

$$\left[\frac{3e^{2x}}{2} + 3e^{-x} \right] - \left[\frac{3e^{2(1)}}{2} + 3e^{-2(1)} \right]$$

$$\left[\frac{3e^4 + 3e^{-1}}{2} \right] - \left[\frac{3e^2 + 3e^{-2}}{2} \right]$$

$$82.30 - 11.490 = \underline{\underline{70.81}}$$

② The parametric equations of a curve are $y = 25\pi x t$ and

$$x = 212t \cos \frac{\pi}{10} t \cdot \text{Find the area under the curve between } t=6$$

$$\text{and } t=10$$

Solution

$$y = 25\pi \frac{x}{10} t \quad t=0$$

$$t=10$$

$$x = 2 + 2t \cos \frac{\pi}{10} t$$

$$\frac{dx}{dt} = -\frac{20}{\pi} \left(\frac{\pi}{10} \right)$$

$$\frac{dx}{dt} = 2t + \frac{20t}{\pi} \sin\left(\frac{\pi}{10}t\right) + \frac{200}{\pi^2} \cos\left(\frac{\pi}{10}t\right)$$

$$\int_0^{10} \left[\frac{20}{\pi} \left(\frac{\pi}{10} \right) \cdot 2t + \frac{20t}{\pi} \sin\left(\frac{\pi}{10}t\right) + \frac{200}{\pi^2} \cos\left(\frac{\pi}{10}t\right) \right] dt$$

$$\left[\frac{20}{\pi} \left(\frac{\pi}{10} \right) \cdot 20(10) + \frac{20(10)}{\pi} \sin\left(\frac{\pi}{10} \times 10\right) + \frac{200}{\pi^2} \cos\left(\frac{\pi}{10} \times 10\right) \right] - \left[\frac{20}{\pi} \left(\frac{\pi}{10} \right) \times 2(0) + \frac{20t}{\pi} \sin\left(\frac{\pi}{10}(0)\right) + \frac{200}{\pi^2} \cos\left(\frac{\pi}{10}(0)\right) \right]$$

$$423.72 - 0 = \underline{\underline{423.72}}$$