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Elect/Elect

18/ENG04048

$$1) A = \int_a^b y \, dx$$

Between two curves

$$A = \int_a^b y_1 \, dx - \int_a^b y_2 \, dx$$

$$A = \int_1^2 3e^{2x} - \int_1^2 3e^{-x}$$

$$A = 3 \left[ \frac{e^{2x}}{2} \right]_1^2 - 3 \left[ -e^{-x} \right]_1^2$$

$$A = 3 \left[ \frac{e^4}{2} - \frac{e^2}{2} \right] - 3 \left[ -e^{-2} - (-e^{-1}) \right]$$

$$A = 70.814 - 3 \left[ -e^{-2} + e^{-1} \right]$$

$$A = 70.814 - 3 \left[ 0.233 \right]$$

$$A = 70.115 \text{ units}$$

$$2) A = \int_a^b y \, dx \quad a=0 \quad b=10$$

$$dx = 2x = \frac{\pi}{5} \sin \frac{\pi}{10} t + dt$$

$$A = \int_0^{10} 8 \sin \frac{\pi}{10} t \left( 2 + \frac{\pi}{5} \sin \frac{\pi}{10} t \right) dt$$

$$= \int_0^{10} 16 \sin \frac{\pi}{10} t + \frac{8\pi}{5} \sin^2 \frac{\pi}{10} t dt$$

$$A = \int_0^{10} 16 \sin \frac{\pi}{10} t + \int_0^{10} \frac{8\pi \sin^2 \frac{\pi}{10} t}{5} dt$$

$$= 4 \int_0^{10} \sin \frac{\pi}{10} t + \frac{2\pi}{5} \int_0^{10} \sin^2 \frac{\pi}{10} t dt$$

$$\left[ -40 \cos \frac{\pi t}{10} \right] + \left[ \frac{2\pi}{5} \cdot \frac{t}{2} - \frac{5 \sin \left( \frac{2\pi t}{10} \right)}{2\pi} \right]_0^{10}$$

$$= \left[ \left[ -40 \cos \frac{\pi(10)}{10} + \pi(10) - \frac{5 \sin \left( \frac{10\pi}{5} \right)}{5} \right] - \left[ -40 \cos \frac{\pi(0)}{10} + \pi(0) - \frac{5 \sin \left( \frac{0}{5} \right)}{5} \right] \right]$$

$$= \left[ \frac{40}{\pi} + 2\pi \right] - \left[ \frac{-40}{\pi} \right]$$

$$= \frac{40}{\pi} + 2\pi + \frac{40}{\pi}$$

$$= \frac{80}{\pi} + \frac{2\pi}{\pi} = \frac{80 + 2\pi}{\pi}$$

$$= 31.74 \text{ square unit}$$