

1a Dynamic equation can refer to the difference equation in discrete differential equation in continuous time. Time scale calculus is combined discrete and continuous time.

1b) An engineering system is described by the expression in equation 1. develop a dynamic model in form of an ordinary differential equation for the system ($y = Ate^t$)

$$y = Ate^t \dots \textcircled{i} \text{ (where } A \text{ is constant)}$$

$$\frac{dy}{dt} = Ate^t \frac{d}{dt}(e^t) + e^t \frac{d}{dt}(At)$$

$$\frac{dy}{dt} = Ate^t + Ae^t \dots \textcircled{ii}$$

From equation (i), make Ae^t the subject of formula

$$y = Ate^t$$

$$\frac{y}{t} = Ae^t \dots \textcircled{iii}$$

put equation (i) and (iii) in equation (ii)

$$\frac{dy}{dt} = \frac{dy}{dt} = y + \frac{y}{t}$$

multiply through by t

$$t \frac{dy}{dt} = ty + y$$

$$t \frac{dy}{dt} = (t + 1)y$$

$$\therefore t \frac{dy}{dt} - (1 + t)y = 0$$