

Wageningen Technological University  
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Electrical/Electronics Engineering  
ENG 382 Assignment I  
ENGINEERING MATHEMATICS II

A flat plate of mass  $m$  falling freely in air with velocity  $v$  is subject to a downward gravitational force and an upward frictional drag force due to air. If the drag force  $F_d$  is given by equation (1),

$$F_d = \frac{0.3v^2}{20 + (\ln v)^3} = 0.02v \quad (1)$$

and the terminal velocity is reached when the drag force equals the gravitational force that is  $F_d = mg$

Taking the values of  $m$  to be 3.5 kg and  $g$  to be  $9.8 \text{ m/s}^2$  using a guess value of  $v_e = 0.5 \text{ m/s}$  and employing fixed point iteration method, develop a MATLAB program, without using "function" command, to estimate the terminal velocity. Use the absolute percentage relative error tolerance to be less than or equal to  $1E-11$ .

SOLUTION:

Command window

```
clear
```

```
clc
```

```
format short
```

```
v = 0.5
```

```
m = 3.5
```

```
g = 9.8
```

```
F = m * g
```

```
v = sqrt(((F + (0.02 * v)) * ((log(v))^3)) + (10 * v) + 17150) / 0.3;
```

```
for i = 1: Inf
```

```
iter(i+1) = i
```

```
v(i+1) = sqrt(((F + (0.02 * v(i))) * ((log(v(i)))^3)) + (10 * v(i)) + 17150) / 0.3;
```

```
fa(i+1) = abs((v(i+1) - v(i)) / v(i+1)) * 100;
```

```
if fa(i+1) <= 1E-11
```

```
break
```

```
end
```

```
end
```

```
table = table(iter, v, fa)
```

# OUTPUT

iter	$\sqrt{\quad}$	$E_n$
0	0.5	
1	239.05	99.77
2	294.17	18.756
3	302.61	2.7894
4	303.85	0.40992
5	304.04	0.060144
6	304.06	0.0088222
7	304.07	0.0012941
8	304.07	0.0001981
9	304.07	2.7842 $\times 10^{-5}$
10	304.07	4.0838 $\times 10^{-6}$
11	304.07	8.7865 $\times 10^{-8}$
12	304.07	1.2888 $\times 10^{-8}$
13	304.07	1.8904 $\times 10^{-9}$
14	304.07	2.7727 $\times 10^{-10}$
15	304.07	4.0679 $\times 10^{-11}$

Converging at iter = 7,  $\sqrt{\quad} = 304.07$

$$F_D = \frac{0.3V^2}{500 + (\ln V)^3} - 0.02V$$

$$F_D = 9.5 \times 3.5 = 34.50 \text{ (use for reference)}$$

substituting  $\sqrt{\quad}$  in  $F_D$

$$F_D = \frac{0.3 \times (304.07)^2}{500 + (\ln 304.07)^3} - 0.02(304.07)$$

$$F_D = 40.38195731 - 6.0814$$

$$F_D = 34.3$$

$\approx$

Proven correct.