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 Electrical/Electronics Engineering
 ENG 382 Assignment 2

A flat plate of mass m falling freely in air with velocity v is subject to a downward gravitational force and an upward potential drag force due to air. If the drag force, F_D is given by equation (1)

$$F_D = 0.3v^2 - 0.02v \quad (1)$$

$500/(4v)^3$

and the terminal velocity is reached when the drag force equals the gravitational force, that is $F_D = mg$

Taking the values of m to be 35kg, g to be 9.8m/s² using a guess value of $v_0 = 0.5$ and employing fixed point iteration method using a MATHEMATICS program without any function command to estimate the terminal velocity. Take the absolute percentage relative error ϵ_a to be less than or equal to 10^{-11}

Solution

Command window

clear

clc

format short

v=0.5

m=35

g=9.8

F=m*g

v = sign(((((F + (0.02 * v)) * (log(v) ^ 3)) + (10 * v) + 17650 / 0.3)))) ;

for i = 1:10^6

if abs(C(i)) <= 10^-11

v(C(i)) = sign(((((F + (0.02 * v(C(i)))) * (log(v(C(i))) ^ 3)) + (10 * v(C(i)) + 17650 / 0.3))))) ;

epsilon_a(C(i)) = abs((((v(C(i) + 1) - v(C(i))) / v(C(i))) * 100)) ;

if epsilon_a(C(i)) <= 10^-11

break

end

end

table = table(C(i), v', epsilon_a')

iter	v	f _n
0	0.5	
1	237.05	99.771
2	294.7	18.736
3	302.61	2.7877
4	303.85	0.40972
5	304.07	0.60144
6	304.07	0.0015222
7	304.07	0.0012541
8	304.07	0.00018781
9	304.07	2.7842e ⁻⁰⁵
10	304.07	4.0835e ⁻⁰⁶
11	304.07	8.7465e ⁻⁰⁸
12	304.07	1.2888e ⁻⁰⁸
13	304.07	1.8709e ⁻⁰⁷
14	304.07	2.7727e ⁻¹⁰
15	304.07	4.0677e ⁻¹¹

converging at iter = 7, v = 304.07

$$f_D = 0.3v^c - 0.02v$$

sqrt(mv)³

$$f_D = 9.8 \times 3.5 = 34.30$$

substituting v into f_D

$$f_D = 0.3 \times (304.07)^c - 0.02(304.07)$$

sqrt(304.07)³

$$f_D = 40.38195731 - 6.0814$$

$$f_D = 34.3$$