



PAL
pensions

MATHS ASSIGNMENT (MAT 104)

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1, $y = 2x^2$ at point (1, 2)

$$\frac{dy}{dx} = 4x$$

$$\left. \frac{dy}{dx} \right|_{x=1} = 4 \cdot 1 = 4$$

$$M = 4$$

$$y - y_1 = M(x - x_1)$$

$$y - 2 = 4(x - 1)$$

$$y - 2 = 4x - 4$$

$y - 4x + 2 = 0$ which gives the equation of tangent
For equation of normal

$$M_1 M_2 = -1$$

$$y_2 - y_1 = M_2(x - x_1)$$

$$y - 2 = \frac{-1}{4}(x - 1)$$

$$4y - 8 = -1(x - 1)$$

$$4y - 8 = -x + 1$$

$4y + x - 9 = 0$ which gives the equation of normal

$$2. y = 3x^2 - 2x \text{ at point } (2, 8)$$

$$\frac{dy}{dx} = 6x - 2$$

$$\left. \frac{dy}{dx} \right|_{x=2} = 6 \cdot 2 - 2 = 10$$

$$\therefore M = 10$$

$$y - y_1 = M(x - x_1)$$

$$y - 8 = 10(x - 2)$$

$$y - 8 = 10x - 20$$

$y - 10x + 12 = 0$ which gives the equation of tangent.

For equation of Normal

$$M_1 M_2 = -1$$

$$10 \cdot M_2 = -1$$

$$M_2 = -\frac{1}{10}$$

$$y - y_1 = M_2(x - x_1)$$

$$y - 8 = -\frac{1}{10}(x - 2)$$

$$10y - 80 = -x + 2$$

$10y + x - 82 = 0$ which gives the equation of the normal.

$$3. y = \frac{x^3}{2} \text{ at point } (-1, -\frac{1}{2})$$

$$\frac{dy}{dx} = \frac{3x^2}{2}$$

$$\left. \frac{dy}{dx} \right|_{x=-1} = \frac{3 \cdot (-1)^2}{2} = \frac{3}{2}$$

$$M = 3$$

$$y - y_1 = M(x - x_1)$$

$$y - [-1/2] = 3/2[x - (-1)]$$

$$2y + 1 = 3x + 3$$

$2y - 3x - 2 = 0$ which gives the equation of tangent

For equation of the normal

$$M_1 M_2 = -1$$

$$\frac{3}{2} \cdot M_2 = -1$$

$$M_2 = -2/3$$

$$M_2 = -2/3$$

$$y - [-1/2] = -2/3[x - (-1)]$$

$$3y + 3/2 = -2x - 2$$

$$3y + 2x + 3/2 + 2 = 0$$

$$3y + 2x + \frac{7}{2} = 0 \text{ which gives } 1$$

$6y + 4x + 7 = 0$ which gives the equation of the normal.

4. $y = 1 + x - x^2$ at point $[-2, -5]$

$$\frac{dy}{dx} = 1 - 2x$$

$$\frac{dy}{dx} \Big|_{x=-2} = 1 - 2 \cdot -2 = 5$$

$$M = 5$$

$$y - y_1 = M(x - x_1)$$

$$y - (-5) = 5[x - (-2)]$$

$$y + 5 = 5x + 10$$

$y - 5x - 5 = 0$ which gives the equation of the tangent

For equation of the normal

$$M_1 M_2 = -1$$

$$5 \cdot M_2 = -1$$

$$M_2 = -1/5$$

$$y - (-5) = -1/5[x - (-2)]$$

$$5y + 25 = -x - 2$$

$5y + x + 27 = 0$ which gives the equation of the normal.

5. $y = 1/x$ at point $(3, 1/3)$

$$y = x^{-1}$$

$$\frac{dy}{dx} = -x^{-2}$$

$$\frac{dy}{dx} \Big|_{x=3} = -3^{-2} = \frac{-1}{3^2} = \frac{-1}{9}$$

$$M = -1/9$$

$$y - y_1 = M_2(x - x_1)$$

$$y - 1/3 = -1/9(x - 3)$$

$$9y - 3 = -x + 3$$

$9y + x - 6 = 0$ which gives the equation of the tangent

For the equation of normal

$$M_1 M_2 = -1$$

$$-1/9 \cdot M_2 = -1$$

$$M_2 = -1 / -1/9 = 9$$

$$y - y_1 = M_2(x - x_1)$$

$$y - 1/3 = 9(x - 3)$$

$$y - 1/3 = 9x - 27$$

$$y - 9x - 1/3 + 27 = 0$$

$$y - 9x + \frac{80}{3} = 0$$

$3y - 27x + 80 = 0$ which gives the equation of normal.