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DEPARTMENT: MEDICINE AND SURGERY

1. $y = 2x^2$ at the point $(1, 2)$

Solution

$$y = 2x^2, \quad \frac{dy}{dx} = 4x$$

$$\left. \frac{dy}{dx} \right|_{x=1} = f(1) = 4$$

$$\therefore m = 4$$

$$x_1 = 1, \quad y_1 = 2$$

$$y - y_1 = m(x - x_1)$$

$$y - 2 = 4(x - 1)$$

$$y - 2 = 4x - 4$$

$$y - 4x - 2 + 4 = 0$$

$$y - 4x + 2 = 0$$

\therefore Equation for the tangent is $y - 4x + 2 = 0$.

For Equation of the normal, $m_1 m_2 = -1$

$$m_2 = \frac{-1}{m_1}$$

$$y - y_1 = \frac{-1}{m} (x - x_1)$$

$$y - 2 = \frac{-1}{4} (x - 1)$$

$$4y - 8 = -x + 1$$

$$4y + x - 8 - 1 = 0$$

\therefore The Equation of the normal is $4y + x - 9 = 0$

2. $y = 3x^2 - 2x$ at the point $(2, 8)$

Solution.

$$\frac{dy}{dx} = 6x - 2$$

$$\left. \frac{dy}{dx} \right|_{x=2} = 6(2) - 2 = 10$$

$$m = 10$$

$$(2, 8) = (x_1, y_1)$$

$$y - y_1 = m(x - x_1)$$

$$y - 8 = 10(x - 2)$$

$$y - 8 = 10x - 20$$

$$y - 10x - 8 + 20 = 0$$

$$y - 10x + 12 = 0$$

∴ The Equation of Tangent is $y - 10x + 12 = 0$

$M_1 M_2 = -1$ (For Equation of the normal)

$$y - y_1 = \frac{-1}{m} (x - x_1)$$

$$y - 8 = \frac{-1}{10} (x - 2)$$

$$10y - 80 = -x + 2$$

$$10y + x - 80 - 2 = 0$$

$$10y + x - 82 = 0.$$

∴ The Equation of the normal is

$$10y + x - 82 = 0.$$

3. $y = \frac{x^3}{2}$ at the point $(-1, -\frac{1}{2})$

Solution.

$$y = \frac{x^3}{2}, \quad \frac{dy}{dx} = \frac{2 \cdot 3x^2 - x^3 \cdot 0}{4}$$

$$\frac{dy}{dx} = \frac{6x^2}{4} = \frac{3x^2}{2}$$

$$\left. \frac{dy}{dx} \right|_{x=-1} = \frac{3(-1)^2}{2}$$

$$m = \frac{3}{2}$$

$$y + \frac{1}{2} = \frac{3}{2}(x + 1)$$

$$2y + 1 = 3x + 3$$

$$2y - 3x + 1 - 3 = 0$$

$$2y - 3x - 2 = 0$$

∴ Equation of the tangent is, $2y - 3x - 2 = 0$

$M_1 M_2 = -1$ (For Equation of the normal)

$$y + \frac{1}{2} = \frac{-1}{\frac{3}{2}} (x + 1)$$

$$y + \frac{1}{2} = -\frac{2}{3}(x + 1)$$

$$3y + \frac{3}{2} = -2x - 2$$

$$6y + 3 = -4x - 4$$

$$6y + 4x + 3 + 4 = 0.$$

$$6y + 4x + 7 = 0.$$

∴ The Equation of the normal is,

$$6y + 4x + 7 = 0$$

4. $y = 1 + x - x^2$ at the point $(-2, 5)$

Solution

$$y = 1 + x - x^2$$

$$\frac{dy}{dx} = 1 - 2x$$

$$\frac{dy}{dx} \Big|_{x=-2} = 1 - 2(-2)$$

$$m = 5$$

For tangent, $y - y_1 = m(x - x_1)$

$$y + 5 = 5(x + 2)$$

$$y + 5 = 5x + 10$$

$$y - 5x + 5 - 10 = 0$$

$$y - 5x - 5 = 0$$

∴ The Equation of tangent is,

$$y - 5x - 5 = 0$$

For normal, $y - y_1 = \frac{-1}{m}(x - x_1)$

$$y + 5 = \frac{-1}{5}(x + 2)$$

$$5y + 5 = -x - 2$$

$$5y + x + 5 + 2 = 0$$

$$5y + x + 7 = 0$$

∴ The equation of the normal,

$$\text{is } 5y + x + 7 = 0$$

5. $y = 1/x$ at the point $(3, 1/3)$

Solution

$$y = 1/x = x^{-1}$$

$$\frac{dy}{dx} = -x^{-2} = -\frac{1}{x^2}$$

$$\frac{dy}{dx} \Big|_{x=3} = -\frac{1}{3^2} = -\frac{1}{9}$$

$$m = -\frac{1}{9}$$

For tangent, $y - y_1 = m(x - x_1)$

$$y - \frac{1}{3} = -\frac{1}{9}(x - 3)$$

$$9y - 3 = -x + 3$$

$$9y - 3 + x - 3 = 0$$

$$9y + x - 6 = 0$$

∴ The equation of the tangent is,

$$9y + x - 6 = 0$$

For normal, $y - y_1 = \frac{-1}{m}(x - x_1)$

$$y - \frac{1}{3} = \frac{-1}{-1/9}(x - 3)$$

$$y - \frac{1}{3} = 9(x - 3)$$

$$y - \frac{1}{3} = 9x - 27$$

$$y - 9x - \frac{1}{3} + 27 = 0$$

$$3y - 27x - 1 + 81 = 0$$

$$3y - 27x + 80 = 0$$

∴ The equation of the normal

$$\text{is } 3y - 27x + 80 = 0$$