

2. $y = 3x^2 - 2x$ at the point $(2, 8)$

Solution

$$\frac{dy}{dx} = 6x - 2$$

$$\left. \frac{dy}{dx} \right|_{x=2} = 6(2) - 2 = 10$$

$$m = 10$$

$$(2, 8) = (x_1, y_1)$$

$$y - y_1 = m(x - x_1)$$

$$y - 8 = 10(x - 2)$$

$$y - 8 = 10x - 20$$

$$y - 10x - 8 + 20 = 0$$

$$y - 10x + 12 = 0$$

\therefore The Equation of Tangent is $y - 10x + 12 = 0$

$M_1 M_2 = -1$ (For Equation of the normal)

$$y - y_1 = \frac{-1}{M_1} (x - x_1)$$

$$y - 8 = \frac{-1}{10} (x - 2)$$

$$10y - 80 = -x + 2$$

$$10y + x - 80 - 2 = 0$$

$$10y + x - 82 = 0$$

\therefore The Equation of the normal is

$$10y + x - 82 = 0$$

3. $y = \frac{x^3}{2}$ at the point $(-1, -\frac{1}{2})$

Solution

$$y = \frac{x^3}{2}, \quad \frac{dy}{dx} = \frac{2 \cdot 3x^2 - x^3 \cdot 0}{4}$$

$$\frac{dy}{dx} = \frac{6x^2}{4} = \frac{3x^2}{2}$$

$$\left. \frac{dy}{dx} \right|_{x=-1} = \frac{3(-1)^2}{2}$$

$$m = \frac{3}{2}$$

$$y + \frac{1}{2} = \frac{3}{2}(x + 1)$$

$$2y + 1 = 3x + 3$$

$$2y - 3x + 1 - 3 = 0$$

$$2y - 3x - 2 = 0$$

\therefore Equation of the tangent is, $2y - 3x - 2 = 0$

$M_1 M_2 = -1$ (For Equation of the normal)

$$y + \frac{1}{2} = \frac{-1}{\frac{3}{2}} (x + 1)$$

$$y + \frac{1}{2} = -\frac{2}{3}(x + 1)$$

$$3y + \frac{3}{2} = -2x - 2$$

$$6y + 3 = -4x - 4$$

$$6y + 4x + 3 + 4 = 0$$

$$6y + 4x + 7 = 0$$

\therefore The Equation of the normal is,

$$6y + 4x + 7 = 0$$