

$$m = 10$$

For the equation of the tangent:

$$y - y_1 = m(x - x_1)$$
$$y - 8 = 10(x - 2)$$

$$y - 8 = 10x - 20$$
$$y - 10x - 8 + 20 = 0$$
$$y - 10x + 12 = 0$$

∴ For the equation of the normal:

$$y - y_1 = -1/m(x - x_1)$$
$$y - 8 = -1/10(x - 2)$$

$$10(y - 8) = -(x - 2)$$
$$10y - 80 = -x + 2$$
$$10y + x - 80 - 2 = 0$$
$$10y + x - 82 = 0$$

3. $y = x^{3/2}$ at the point $(-1, -1/2)$

For the normal:

$$y = x^{3/2}$$
$$\frac{dy}{dx} \text{ of } \frac{1}{2} x^3 = \frac{3x^2}{2}$$

$$\left. \frac{dy}{dx} \right|_{x=-1} = \frac{3}{2} (-1)^2 = \frac{3}{2} \times 1$$

$$m = dy/dx = 3/2$$

For the equation of the tangent:

$$y - y_1 = m(x - x_1)$$
$$y - (-1/2) = m(x - (-1))$$

$$y + \frac{1}{2} = m(x + 1)$$
$$y + \frac{1}{2} = \frac{3}{2}(x + 1)$$

(multiply both sides by 2)

$$2(y + \frac{1}{2}) = 3(x+1)$$

$$2y + 1 = 3(x+1)$$

$$2y + 1 = 3x + 3$$

$$2y - 3x + 1 - 3 = 0$$

$$2y - 3x - 2 = 0$$

For the equation of the normal:

$$y - y_1 = -1/m (x - x_1)$$

$$y + \frac{1}{2} = -1/3/2 (x - C - 1)$$

$$y + \frac{1}{2} = -\frac{2}{3} (x + 1)$$

(multiply both sides by 6)

$$6(y + \frac{1}{2}) = 6(-\frac{2}{3}(x + 1))$$

$$6y + 3 = -4(x + 1)$$

$$6y + 3 = -4x - 4$$

$$6y + 4x + 3 + 4 = 0$$

$$\therefore 6y + 4x + 7 = 0$$

4. $y = 1 + x - x^2$ at the point $C(-2, -5)$

For normal;

$$y = 1 + x - x^2$$

$$\frac{dy}{dx} = 1 - 2x$$

$$\frac{dy}{dx} \Big|_{x=-2} = 1 - 2(-2)$$

$$= 1 + 4$$

$$m_t = dy/dx = 5$$

For equation of tangent

$$y - y_1 = m(x - x_1)$$

$$y - (-5) = 5(x - (-2))$$

$$y + 5 = 5(x + 2)$$

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MAT104

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Assignment

1. $y = 2x^2$ at the point $(1, 2)$

For the normal:

$$y = 2x^2$$

$$\frac{dy}{dx} = 4x$$

$$\frac{dy}{dx} \Big|_{x=1} = 4(1) = 4$$

For the equation of tangent:

$$y - y_1 = m(x - x_1)$$

$$y - 2 = 4(x - 1)$$

$$y - 2 = 4x - 4$$

$$y - 2 - 4x + 4 = 0$$

$$y - 4x + 2 = 0$$

$$\therefore y - 4x + 2 = 0$$

For the equation of the normal:

$$y - y_1 = -\frac{1}{m}(x - x_1)$$

$$y - 2 = -\frac{1}{4}(x - 1)$$

$$4(y - 2) = -1(x - 1)$$

$$4y - 8 = -x + 1$$

$$4y + x - 9 = 0$$

$$\therefore 4y + x - 9 = 0$$

2. $y = 3x^2 - 2x$, at the point $(2, 8)$

For the normal:

$$y = 3x^2 - 2x$$

$$\frac{dy}{dx} = 6x - 2$$

$$\frac{dy}{dx} \Big|_{x=2} = 6(2) - 2$$

$$\frac{dy}{dx} \Big|_{x=2} = 10$$

$$\therefore \frac{dy}{dx} = 10$$

$$y+5 = 5x+10$$

$$y-5x+5-10=0$$

$$y=5x-5=0$$

For equation of normal

$$y-y_1 = -1/m(x-x_1)$$

$$y-(-5) = -1/5(x-(-2))$$

$$y+5 = -1/5(x+2)$$

$$5(y+5) = -1(x+2) \quad (\text{multiply through by 5})$$

$$5y+25 = -x-2$$

$$5y+x+27=0$$

5) $y = 1/x$ at the point $C(3, 1/3)$

For the normal

$$x=3, y=1/3$$

$$y = 1/x$$

$$y = x^{-1}$$

$$\frac{dy}{dx} = -x^{-2}$$

$$m = -(3)^{-2} = 1/3^2 = 1/9$$

For the equation of the tangent

$$y-y_1 = m(x-x_1)$$

$$(y-1/3) = +1/9(x-3) \quad (\text{multiply through by 9})$$

$$9y-3 = 1(x-3)$$

$$9y-3 = x-3$$

$$9y+x-3-3=0$$

$$9y+x-6=0$$

For equation of the normal

$$y-y_1 = -1/m(x-x_1)$$

$$(y-1/3) = 9(x-3) \quad (\text{multiply through by 9})$$

$$3y-1 = 27(x-3)$$

$\frac{27}{62}$

$$3y - 1 = 27x - 72$$

$$3y - 1 = 27x - 81$$

$$3y - 27x - 1 + 81 = 0$$

$$\therefore 3y - 27x + 80 = 0$$