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1  $y = 2x^2$  at the point  $(1, 2)$

Soln

Equation Of Tangent

$$y = 2x^2$$

$$\frac{dy}{dx} = 4x$$

$$\left. \frac{dy}{dx} \right|_{x=1} = 4(1) = 4$$

$$\therefore m = 4$$

$$y - y_1 = m(x - x_1)$$

$$y - 2 = 4(x - 1)$$

$$y - 2 = 4x - 4$$

$$y - 4x + 2 + 4 = 0$$

$$y - 4x + 2 = 0$$

b Equation Of Normal

$$m_1 m_2 = -1$$

$$y - y_1 = \frac{-1}{m} (x - x_1)$$

$$y - 2 = \frac{-1}{4} (x - 1)$$

$$4y - 8 = -x + 1$$

$$4y - 8 + x - 1 = 0$$

$$4y + x - 9 = 0$$

2  $y = 3x^2 - 2x$  at the point  $(2, 8)$

$$\frac{dy}{dx} = 6x - 2$$

$$\left. \frac{dy}{dx} \right|_{x=2} = 6(2) - 2 = 10$$

$$\therefore m = 10$$

$$m_1, m_2 = -1$$

$$y - y_1 = \frac{1}{m} (x - x_1)$$

$$y - 8 = 10(x - 2)$$

$$y - 8 = 10x - 20$$

$$y - 10x - 8 + 20 = 0 = y - 10x + 12 = 0$$

$$\therefore y - 10x + 12 = 0 \text{ [Equation Of The Normal]}$$

Equation To The Tangent

$$y - y_1 = \frac{-1}{m} (x - x_1)$$

$$y - 8 = \frac{-1}{10} (x - 2)$$

$$10y - 80 = -x + 2$$

$$10y + x - 82 = 0$$

3  $y = \frac{x^3}{2}$  at the point of  $(-1, -1/2)$

Equation Of The Normal

$$y = \frac{x^3}{2}$$

$$\frac{dy}{dx} = \frac{3x^2}{2}$$

$$\left. \frac{dy}{dx} \right|_{x=-1} = \frac{3(-1)^2}{2} = \frac{3}{2}$$

$$\therefore m = \frac{3}{2}$$

$$\therefore m = \frac{3}{2}$$

$$y - y_1 = m(x - x_1)$$

$$y - (-1/2) = \frac{3}{2}(x - (-1))$$

5  $y = \frac{1}{x}$  at the point  $(3, \frac{1}{3})$

$$\frac{dy}{dx} = \frac{x^{-1}}{x^2}$$

$$\left. \frac{dy}{dx} \right|_{x=3} = \frac{-1}{3^2} = \frac{-1}{9}$$

$$\therefore m = \frac{-1}{9}$$

$$y - y_1 = m(x - x_1)$$
$$y - \frac{1}{3} = \frac{-1}{9}(x - 3)$$

$$y - \frac{1}{3} = -\frac{x}{9} + \frac{1}{3}$$

$$y - \frac{1}{3} + \frac{x}{9} - \frac{1}{3} = 0$$

$$y + \frac{x}{9} - \frac{2}{3} = 0 \quad [\text{Equation of The Normal}]$$

Equation Of The Tangent

$$y - y_1 = \frac{-1}{m}(x - x_1)$$

$$(m_2 = \frac{-1}{m} = m_2 = \frac{-k}{-1/9} = 9)$$

$$y - \frac{1}{3} = 9(x - 3)$$

$$y - 9x - \frac{1}{3} + 27 = 0$$

$$y - 9x + \frac{80}{3} = 0$$

$$y + \frac{1}{2} = -x - 1$$

$$3y + \frac{3}{2} = -x - 1$$

$$3y + x + \frac{3}{2} + 1 = 0$$

$$3y + x + \frac{5}{2} = 0$$

4  $y = 1 + x - x^2$  at the point  $(-2, -5)$   
Equation At The Normal

$$y = 1 + x - x^2$$

$$\frac{dy}{dx} = 1 - 2x$$

$$\left. \frac{dy}{dx} \right|_{x=-2} = 1 - 2(-2) = 1 + 4 = 5$$

$$\therefore m = 5$$

$$y - y_1 = m(x - x_1)$$

$$y - (-5) = 5(x - (-2))$$

$$y + 5 = 5x + 10$$

$$y + 5 = 5x + 10$$

$$y + 5 - 5x - 10 = 0$$

$$y - 5x - 5 = 0$$

Equation At the Tangent

$$y - y_1 = \frac{-1}{m}(x - x_1)$$

$$y - (-5) = \frac{-1}{5}(x - (-2))$$

$$y + 5 = -\frac{1}{5}(x + 2)$$

$$5y + 25 = -x - 2$$

$$5y + x + 25 + 2 = 0$$

$$5y + x + 27 = 0$$