

GWARAM, MUBARAK.....19/MHS01/249.....MBBS.....MAT 104 ASSIGNMENT

Course: Mat 104  
College: MHS

Assignment Solution

1)  $y = 2x^2$  (1, 2)  
 $m = \frac{dy}{dx} = 4x$ ;  $x = 1$ ;  $m = 4 \times 1 = 4$

Equation of tangent;  
 $y - y_1 = m(x - x_1)$   
 $y - 2 = 4(x - 1)$   
 $y - 2 = 4x - 4$   
 $y - 2 = 4(x - 1)$   
 $y - 2 = 4x - 4$   
 $4x - 2 + 4 = 0$   
 $y - 4x + 2 = 0$

Eqn of normal  
 $y - y_1 = -\frac{1}{m}(x - x_1)$   
 $y - 2 = -\frac{1}{4}(x - 1)$   
 $y - 2 = -\frac{x}{4} + \frac{1}{4}$   
 $y + \frac{x}{4} - 2 - \frac{1}{4} = 0$   
 $y + \frac{x}{4} - \frac{9}{4} = 0$

multiply through by 4  
 $4y + x - 9 = 0$

2)  $y = 3x^2 - 2x$  (2, 8)  
 $m = \frac{dy}{dx} = 6x - 2$   
 where  $x = 2$ ;  $m = 6(2) - 2 = 12 - 2 = 10$

Equation of tangent;  
 $y - y_1 = m(x - x_1)$   
 $y - 8 = 10(x - 2)$

Continuation of No 2  
 $y - 8 = 10x - 20$   
 $y - 10x + 12 = 0$

Equation of normal  
 $y - y_1 = -\frac{1}{m}(x - x_1)$   
 $y - 8 = -\frac{1}{10}(x - 2)$   
 $y - 8 = -\frac{x}{10} + \frac{2}{10}$   
 $y + \frac{x}{10} - \frac{82}{10} = 0$   
 $10y + x - 82 = 0$

3)  $y = x^3/2$  (-1, -1/2)  
 $m = \frac{dy}{dx} = \frac{1}{2} \times 3x^2 = \frac{3}{2}x^2$   
 where  $x = -1$ ;  $m = \frac{3}{2}(-1)^2 = \frac{3}{2}$

Equation of tangent  
 $y - y_1 = m(x - x_1)$   
 $y - (-\frac{1}{2}) = \frac{3}{2}(x - (-1))$   
 $y + \frac{1}{2} = \frac{3}{2}(x + 1)$   
 $y + \frac{1}{2} = \frac{3}{2}x + \frac{3}{2}$   
 $y - \frac{3}{2}x - 1 = 0$   
 $2y - 3x - 2 = 0$

Equation of normal  
 $y - y_1 = -\frac{1}{m}(x - x_1)$   
 $y - (-\frac{1}{2}) = -\frac{2}{3}(x - (-1))$   
 $y + \frac{1}{2} = -\frac{2}{3}(x + 1)$   
 $y + \frac{1}{2} = -\frac{2}{3}x - \frac{2}{3}$   
 $3y + \frac{3}{2}x + \frac{7}{6} = 0$   
 $6y + 4x + 7 = 0$

4)  $y = 1 + x - x^2$  (-2, -5)  
 $m = \frac{dy}{dx} = 1 - 2x$   
 where  $x = -2$ ;  $m = 1 - 2(-2) = 5$

Equation of tangent  
 $y - y_1 = m(x - x_1)$   
 $y - (-5) = 5(x - (-2))$   
 $y + 5 = 5(x + 2)$   
 $y + 5 = 5x + 10$   
 $y - 5x - 5 = 0$

Equation of normal  
 $y - y_1 = -\frac{1}{m}(x - x_1)$   
 $y - (-5) = -\frac{1}{5}(x - (-2))$   
 $y + 5 = -\frac{1}{5}(x + 2)$   
 $y + 5 = -\frac{x}{5} - \frac{2}{5}$   
 $y + \frac{x}{5} + \frac{27}{5} = 0$   
 $5y + x + 27 = 0$

5)  $y = 1/x$  (3, 1/3)  
 $m = \frac{dy}{dx} = x^{-2} = -x^{-3}$   
 where  $x = 3$ ;  $m = -(3)^{-2} = -1/9$

Equation of tangent  
 $y - y_1 = m(x - x_1)$   
 $y - \frac{1}{3} = -\frac{1}{9}(x - 3)$   
 $y - \frac{1}{3} = -\frac{x}{9} + \frac{1}{3}$   
 $y + \frac{x}{9} - \frac{2}{3} = 0$   
 $9y + x - 6 = 0$

Equation of normal  
 $y - y_1 = -\frac{1}{m}(x - x_1)$   
 $y - \frac{1}{3} = 9(x - 3)$   
 $y - \frac{1}{3} = 9x - 27$

Continuation of No. 5  
 $y - 9x + \frac{80}{3} = 0$   
 Multiply through by 3  
 $3y - 27x + 80 = 0$