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Course: Mat 104
College: MHS

Assignment Solution

1) $y = 2x^2$ (1, 2)
 $m = \frac{dy}{dx} = 4x$; $x = 1$; $m = 4 \times 1 = 4$

Equation of tangent;
 $y - y_1 = m(x - x_1)$
 $y - 2 = 4(x - 1)$
 $y - 2 = 4x - 4$
 $y - 2 = 4(x - 1)$
 $y - 2 = 4x - 4$
 $4x - 2 + 4 = 0$
 $y - 4x + 2 = 0$

Eqn of normal
 $y - y_1 = -\frac{1}{m}(x - x_1)$
 $y - 2 = -\frac{1}{4}(x - 1)$
 $y - 2 = -\frac{x}{4} + \frac{1}{4}$
 $4y + x - 2 - \frac{1}{4} = 0$
 $4y + x - \frac{9}{4} = 0$

multiply through by 4
 $4y + x - 9 = 0$

2) $y = 3x^2 - 2x$ (2, 8)
 $m = \frac{dy}{dx} = 6x - 2$
 where $x = 2$; $m = 6(2) - 2 = 12 - 2 = 10$

Equation of tangent;
 $y - y_1 = m(x - x_1)$
 $y - 8 = 10(x - 2)$

Continuation of No 2
 $y - 8 = 10x - 20$
 $y - 10x + 12 = 0$

Equation of normal
 $y - y_1 = -\frac{1}{m}(x - x_1)$
 $y - 8 = -\frac{1}{10}(x - 2)$
 $y - 8 = -\frac{x}{10} + \frac{2}{10}$
 $y + \frac{x}{10} - \frac{82}{10} = 0$
 $10y + x - 82 = 0$

3) $y = x^2/2$ (-1, -1/2)
 $m = \frac{dy}{dx} = \frac{1}{2} \times 2x = x$
 where $x = -1$; $m = \frac{1}{2}(-1) = -\frac{1}{2}$

Equation of tangent
 $y - y_1 = m(x - x_1)$
 $y - (-\frac{1}{2}) = -\frac{1}{2}(x - (-1))$
 $y + \frac{1}{2} = -\frac{1}{2}(x + 1)$
 $y + \frac{1}{2} = -\frac{x}{2} - \frac{1}{2}$
 $y - \frac{1}{2}x - 1 = 0$
 $2y - 3x - 2 = 0$

Equation of normal
 $y - y_1 = -\frac{1}{m}(x - x_1)$
 $y - (-\frac{1}{2}) = -\frac{1}{-1/2}(x - (-1))$
 $y + \frac{1}{2} = 2(x + 1)$
 $y + \frac{1}{2} = 2x + 2$
 $3y + \frac{1}{2}x - \frac{7}{2} = 0$
 $6y + 4x - 7 = 0$

4) $y = 1 + x - x^2$ (-2, -5)
 $m = \frac{dy}{dx} = 1 - 2x$
 where $x = -2$; $m = 1 - 2(-2) = 5$

Equation of tangent
 $y - y_1 = m(x - x_1)$
 $y - (-5) = 5(x - (-2))$
 $y + 5 = 5(x + 2)$
 $y + 5 = 5x + 10$
 $y - 5x - 5 = 0$

Equation of normal
 $y - y_1 = -\frac{1}{m}(x - x_1)$
 $y - (-5) = -\frac{1}{5}(x - (-2))$
 $y + 5 = -\frac{1}{5}(x + 2)$
 $y + 5 = -\frac{x}{5} - \frac{2}{5}$
 $5y + \frac{x}{5} + \frac{27}{5} = 0$
 $5y + x + 27 = 0$

5) $y = 1/x$ (3, 1/3)
 $m = \frac{dy}{dx} = -x^{-2} = -\frac{1}{x^2}$
 where $x = 3$; $m = -\frac{1}{3^2} = -\frac{1}{9}$

Equation of tangent
 $y - y_1 = m(x - x_1)$
 $y - \frac{1}{3} = -\frac{1}{9}(x - 3)$
 $y - \frac{1}{3} = -\frac{x}{9} + \frac{1}{3}$
 $y + \frac{x}{9} - \frac{2}{3} = 0$
 $9y + x - 6 = 0$

Equation of normal
 $y - y_1 = -\frac{1}{m}(x - x_1)$
 $y - \frac{1}{3} = 9(x - 3)$
 $y - \frac{1}{3} = 9x - 27$

Continuation of No. 5
 $y - 9x + \frac{80}{3} = 0$
 Multiply through by 3
 $3y - 27x + 80 = 0$