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DEPT :- MEBS
COURSE CODE :- MATHS 148

(1) $y = 2x^2$ at points $(1, 2)$
(a) The equation at tangent

$$\frac{dy}{dx} = 4x$$

$$m_1 = \frac{dy}{dx}\Big|_{x = x_1}$$

$$m_1 = 4(1) = 4$$

$$y - y_1 = m(x - x_1)$$
$$y - 2 = 4(x - 1)$$
$$y - 2 = 4x - 4$$

$y - 4x + 2 = 0$ is the equation at tangent

(b) The equation at normal

$$m_2 = \frac{-1}{m_1} = \frac{-1}{4}$$

$$y - y_1 = \frac{-1}{m_1}(x - x_1)$$

$$y - 2 = \frac{-1}{4}(x - 1)$$

$$4(y - 2) = -1(x - 1)$$
$$4y - 8 = -x + 1$$

$4y + x - 9 = 0$ is the equation at normal

(2) $y' = 3x^2 - 2x$ [illegible]

$$\frac{dy}{dx}\Big|_{x = -1} = \frac{6(-1)^2}{4}$$

$$m = 6/4 = 3/2$$

$y + 1/2 = 3/2(x + 1)$ (divide through by 2)

$$2y + 1 = 3(x + 1)$$
$$2y - 3x = 0$$
$$2y - 3x = 0$$

∴ Equation of the tangent is $2y - 3x = 0$

$$y - y_1 = \frac{-1}{m_1}(x - x_1)$$

$$y + 1/2 = -2/3(x + 1)$$
$$y + 1/2 = -2/3x - 2/3$$
$$y + 2/3x + 7/6 = 0$$

Divide through by 6

$6y + 4x + 7 = 0$ is the equation of the normal

(3) $y = 1 + x - x^2$ at the point $(2, -5)$
(a) the equation at tangent

$$\frac{dy}{dx} = -2x + 1$$

$$m_1 = \frac{dy}{dx}\Big|_{x = x_1}$$

$$m_1 = -2(-2) + 1 = 5$$
$$y - y_1 = m_1(x - x_1)$$
$$y + 5 = 5(x + 2)$$
$$y + 5 = 5x + 10$$

$y - 5x - 5 = 0$ is the equation of tangent

(2) $y = 3x^2 - 2x$ at the points $(2, 8)$

(i) for the equation at tangent :-

$\frac{dy}{dx} = 6x - 2$

$m_1 = \frac{dy}{dx} \Big|_{x = x_1}$

$m_1 = 6(2) - 2$

$m_1 = 10$

$y - y_1 = m(x - x_1)$

$y - 8 = 10(x - 2)$

$y - 8 = 10x - 20$

$\therefore y - 10x + 12 = 0$ is the equation at tangent

for the equation at normal

$m_2 = \frac{-1}{m_1} = \frac{-1}{10}$

$y - y_1 = \frac{-1}{m_1}(x - x_1)$

$y - 8 = \frac{-1}{10}(x - 2)$

$10(y - 8) = -1(x - 2)$

$10y - 80 = -x + 2$

$10y + x - 82 = 0$ is equation at normal

(3) $y = \frac{x^3}{2}$ $(-1, -\frac{1}{2})$

$\frac{dy}{dx} = \frac{V\, du/dx - U\, dv/dx}{V^2}$ let $V = 2$ & $u = x^3$

$= \frac{6x^2 - x^3 \cdot 0}{2^2} = \frac{6x^2 - 0}{4}$ $\therefore \frac{dy}{dx} = \frac{6x^2}{4}$

(4) for the equation at normal

$m_2 = \frac{-1}{m_1} = \frac{-1}{5}$

$y - y_1 = m_2(x - x_1)$

$y + 5 = \frac{-1}{5}(x + 2)$

$5(y + 5) = -1(x + 2)$

$5y + 25 = -x - 2$

$\therefore 5y + x + 27 = 0$ is equation at normal

(5) $y = \frac{1}{x}$ $(3, \frac{1}{3})$

$y = x^{-1}$

$dy/dx = -x^{-2}$

$m_1 = (-3)^{-2} = -\frac{1}{9}$

$\frac{dy}{dx}\Big|_{x=3} = -\frac{1}{9}$

$y - y_1 = m(x - x_1)$

$y - \frac{1}{3} = -\frac{1}{9}(x - 3)$

$9y - 3 = -1(x - 3)$

$9y + x - 6 = 0$ is equation of the tangent

(6) $y - y_1 = -\frac{1}{m_1}(x - x_1)$

$\therefore y - \frac{1}{3} = -(-9)(x - 3)$

$y - \frac{1}{3} = 9(x - 3)$

$3y - 1 = 27(x - 3)$

$3y - 1 = 27x - 81$

$3y - 27x + 80$