

4. $y = 1 + 2 - x^2$ at the point $(-2, 5)$

$$y = -x^2 + x + 1$$

multiply through by -1

$$y = x^2 - x - 1$$

$$\frac{dy}{dx} = 2x - 1$$

$$\text{at } m = 2(-2) - 1$$

$$m = -5$$

$$y - y_1 = m(x - x_1)$$

$$y + 5 = -5(x + 2)$$

$$y + 5 = -5x - 10$$

$$y + 5 + 5x + 10 = 0$$

$$5x + y + 15 = 0 \text{ (eqn of the tangent)}$$

eq normal $m_2 = -1$

$$y - y_1 = -1/m(x - x_1)$$

$$y + 5 = -1/5(x + 2)$$

$$\frac{y + 5}{1} = \frac{x + 2}{5}$$

$$x + 2 = 5(y + 5)$$

$$x + 2 - 5y - 25 = 0$$

$$x - 5y - 23 = 0 \text{ (eqn of the normal)}$$

5. $y = 1/x$ at the point $(3, 1/3)$

$$y = x^{-1}$$

$$\frac{dy}{dx} = -x^{-2}$$

$$\text{at } m = -(3)^{-2} = m = -0.11$$

$$y - y_1 = m(x - x_1) \Rightarrow y - 1/3 = -0.11(x - 3)$$

$$y - 1/3 = -0.11x + 0.33$$

$$y - 1/3 + 0.11x - 0.33 = 0$$

$$0.11x + y - 0.66 = 0 \text{ (eqn of the tangent)}$$

6. at the normal.

$$y - y_1 = m(x - x_1)$$

$$y - 1/3 = -1/5(x - 3)$$

$$\frac{y - 1/3}{1} = \frac{x - 3}{5}$$

$$x - 3 = 5(y - 1/3)$$

$$x - 3 = 5y - 1.667$$

$$x - 5y + 1.667 = 0$$

eqn of the normal

$$y - 5 = \frac{-x + 2}{10}$$

$$-x + 2 = 10(y - 5)$$

$$-x + 2 = 10y - 50$$

$$10y - x - 52 = 0$$

center at the normal

3.

$y = x/2$ at the point $(-1, -1/2)$

$$y = 2x - 3$$

$$m = \frac{dy}{dx} = -6x + 2$$

$$m = -6(-1) = 6$$

$$m = -6$$

$$y - y_1 = m(x - x_1)$$

$$y + 1/2 = -6(x + 1)$$

$$y + 1/2 + 6x + 6 = 0$$

$$6x + y + 13/2 = 0$$

Multiply through by 2

$$12x + 2y + 13 = 0$$

center at the tangent

at the normal $m = -1/6$

$$y - y_1 = -1/6(x - x_1)$$

$$y + 1/2 = -1/6(x + 1)$$

$$y + 1/2 = \frac{-x - 1}{6}$$

$$x + 1 = 6(y + 1/2)$$

$$x + 1 = 6y + 3$$

$$x + 1 - 6y - 3 = 0$$

$$x - 6y - 2 = 0 \text{ (center at the normal)}$$

$$1. \quad y = 2x^2 \text{ at point } (1, 2)$$

$$\frac{dy}{dx} = 4x$$

$$m = 4$$

$$y - y_1 = m(x - x_1)$$

$$y - 2 = 4(x - 1)$$

$$y - 2 = 4x - 4$$

$$y - 2 - 4x + 4 = 0$$

at normal $m_1 m_2 = -1$

$$y - y_1 = -\frac{1}{m}(x - x_1)$$

$$y - 2 = -\frac{1}{4}(x - 1)$$

$$y - 2 = \frac{-x + 1}{4}$$

$$-x + 1 = 4(y - 2)$$

$$-x + 1 - 4y + 8 = 0$$

~~4y + x - 9 = 0~~, (read at the normal).

$$2. \quad y = 3x^2 - 2x \text{ at the point } (2, 8)$$

$$\frac{dy}{dx} = 6x - 2$$

$$m = 6(2) - 2$$

$$= 12 - 2 = 10$$

$$y - y_1 = m(x - x_1)$$

$$y - 8 = 10(x - 2)$$

$$y - 8 - 10x + 20 = 0$$

$y - 10x + 12 = 0$ (read at the tangent).

at the normal $m_1 m_2 = -1$

$$y - y_1 = -\frac{1}{m}(x - x_1)$$

$$y - 8 = -\frac{1}{10}(x - 2)$$