

1. Find the Limit of the function

$$\left\{ \frac{x - \cos x}{x} \right\} \text{ as } x \rightarrow 0$$

Using L'Hopital's Rule

$$\lim_{x \rightarrow 0} \left\{ \frac{1 - (-\sin x)}{1} \right\}$$

$$\lim_{x \rightarrow 0} \left\{ \frac{1 + \sin x}{1} \right\} = \frac{1 + \sin 0}{1} = \frac{1 + 0}{1} = 1$$

2. If $y = -3 \tan 7x e^{3x}$, find $\frac{dy}{dx}$

Let $u = -3 \tan 7x$, $v = e^{3x}$
 $\frac{du}{dx} = -21 \sec^2 7x$, $\frac{dv}{dx} = 3e^{3x}$

$$\therefore \frac{dy}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$$

$$\begin{aligned} \therefore \frac{dy}{dx} &= (-3 \tan 7x)(3e^{3x}) + (e^{3x})(-21 \sec^2 7x) \\ &= -9 \tan 7x e^{3x} - 21 \sec^2 7x e^{3x} \end{aligned}$$

3. If $y = \cos 3x$, Find $\frac{dy}{dx}$ using first principles.

$$y = \cos 3x$$

$$y + \Delta y = \cos(3x + 3\Delta x)$$

$$\Delta y = \cos(3x + 3\Delta x) - \cos 3x$$

Recall that $\cos A - \cos B = -2 \sin \frac{A+B}{2} \sin \frac{A-B}{2}$

$$\Delta y = -2 \sin \frac{3x + 3\Delta x + 3x}{2} \sin \frac{3x + 3\Delta x - 3x}{2}$$

$$\Delta y = -2 \sin \frac{6x + 3\Delta x}{2} \sin \frac{3\Delta x}{2}$$

$$\frac{\Delta y}{\Delta x} = \frac{-2 \sin \frac{6x + 3\Delta x}{2} \sin \frac{3\Delta x}{2}}{\Delta x} \text{ multiply by } \frac{1}{2}$$

Δx

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$$\frac{\Delta y}{\Delta x} = \frac{-2 \sin 6x + 3\Delta x}{2} \frac{\sin 3\Delta x}{2} \times 1$$

$$\frac{\Delta y}{\Delta x} = \frac{-\sin \frac{6x+3\Delta x}{2} \sin \frac{3\Delta x}{2}}{\frac{\Delta x}{2}} = \frac{-\sin \frac{3}{2} \frac{6x+3\Delta x}{2} + \frac{3\Delta x}{2} \sin \frac{3\Delta x}{2}}{\frac{\Delta x}{2}}$$

$$\lim_{\Delta x \rightarrow 0} \frac{\Delta y}{\Delta x} = -\sin(3x+0) \cdot \frac{\sin 3\Delta x}{\frac{\Delta x}{2}}$$

$$\text{Since } \lim_{\Delta x \rightarrow 0} \frac{\sin \frac{3\Delta x}{2}}{\frac{\Delta x}{2}} = 3(1) = 3$$

$$\therefore \frac{dy}{dx} = -3 \sin 3x$$

4. Given that $f(x) = 2x^3 - 7x$ and $g(x) = -3x$, find $(f-g)(5)$

$$\begin{aligned}(f-g)(5) &= 2x^3 - 7x - (-3x) \\ &= 2x^3 - 7x + 3x \\ &= 2x^3 - 4x \\ &= 2(5)^3 - 4(5) \\ &= 250 - 20 = \underline{230}\end{aligned}$$

5. Find $f \circ g(x)$, if $f(x) = 4x^2 + 2$ and $g(x) = 2x + 3$.

$$\begin{aligned}f \circ g(x) &= 4(2x+3)^2 + 2 \\ &= 4(4x^2 + 6x + 6x + 9) + 2 \\ &= 4(4x^2 + 12x + 9) + 2 \\ &= 16x^2 + 48x + 36 + 2 \\ &= 16x^2 + 48x + 38\end{aligned}$$

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6. Find the gradient of $x^2 + 2xy + y^2 = 1,020$

$$x^2 + 2xy + y^2 = 1,020$$

$$2x \frac{dx}{dx} + 2x \frac{dy}{dx} + 2y \frac{dx}{dx} + 2y \frac{dy}{dx} = 0$$

$$2x + 2x \frac{dy}{dx} + 2y + 2y \frac{dy}{dx} = 0$$

$$\frac{dy}{dx} (2x + 2y) = -2x - 2y$$

$$\therefore \frac{dy}{dx} = \frac{-2x - 2y}{2x + 2y}$$

7. Find the first derivative of the function $y = x^2 \cos x$

$$y = x^2 \cos x$$

$$\text{let } u = x^2, v = \cos x$$

$$\frac{du}{dx} = 2x, \frac{dv}{dx} = -\sin x$$

$$\frac{dy}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$$

$$\frac{dy}{dx} = (x^2)(-\sin x) + (\cos x)(2x)$$

$$\frac{dy}{dx} = -x^2 \sin x + 2x \cos x$$