

UKANDA NINECOMA GEN

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MAT 104 ASSIGNMENT

10) For the curves in problem 1 to 5 at the points given, find
a) the equation of the tangent and b) the equation of the normal.

1) $y = 2x^2$ at the point $(1, 2)$.

$$\frac{dy}{dx} = 4x$$

$$\frac{dy}{dx} \text{ at } x=1 = 4(1) = 4$$

$$m = 4$$

$$x_1 = 1$$

$$y_1 = 2$$

Equation of a tangent

$$y - y_1 = m(x - x_1)$$

$$y - 2 = 4(x - 1)$$

$$y - 2 = 4x - 4$$

$$y = 4x - 2$$

Equation of the normal

$$m_2 = -\frac{1}{m_1}$$

$$m_2 = -\frac{1}{4}$$

$$y - y_1 = m_2(x - x_1)$$

$$y - 2 = -\frac{1}{4}(x - 1)$$

$$y - 2 = -\frac{1}{4}x + \frac{1}{4}$$

$$y - 2 = \frac{-x + 1}{4}$$

$$4y - 8 = -x + 1$$

$$4y + x - 8 - 1 = 0$$

$$4y + x - 9 = 0$$

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$$2) \quad y = 3x^2 - 2x \text{ at the point } (2, 8)$$
$$\frac{dy}{dx} = 6x - 2$$
$$\frac{dy}{dx} \Big|_{x=2} = 6(2) - 2 = 12 - 2 = 10$$
$$m = 10$$

Eqn of tangent

$$y - y_1 = m(x - x_1)$$

$$y - 8 = 10(x - 2)$$

$$y - 8 = 10x - 20$$

$$y - 8 - 10x + 20 = 0$$

$$y - 10x + 12 = 0$$

Eqn of normal

$$y - y_1 = -\frac{1}{m}(x - x_1)$$

$$y - 8 = -\frac{1}{10}(x - 2)$$

$$y - 8 = \frac{-x + 2}{10}$$

$$10y - 80 = -x + 2$$

$$10y + x - 80 - 2 = 0$$

$$10y + x - 82 = 0$$

$$3) \quad y = \frac{x^3}{2} \text{ at point } (-1, -\frac{1}{2})$$
$$\frac{dy}{dx} = \frac{3x^2}{2}$$

$$\frac{dy}{dx} \Big|_{x=-1} = \frac{3(-1)^2}{2} = \frac{3}{2}$$

$$m = \frac{3}{2}$$

Eqn of tangent

$$y - y_1 = m(x - x_1)$$

$$y - (-\frac{1}{2}) = \frac{3}{2}(x - (-1))$$

$$y + \frac{1}{2} = \frac{3}{2}(x + 1)$$

$$2y + 1 = 3x + 3$$

$$2y = 3x + 2$$

$$2y - 3x - 2 = 0$$

Equation of normal

$$y - y_1 = m(x - x_1)$$

$$y + 6 = -\frac{2}{3}(x + 1)$$

$$6y + 3 = -4x - 4$$

$$6y + 3 + 4x + 4 = 0$$

$$6y + 4x + 7 = 0$$

4) $y = 1 + x - x^2$ at the point $(-2, -5)$.

$$\frac{dy}{dx} = m(1 - 2x)$$

$$m = 1 - 2x \text{ at } x = -2 \quad 1 - 2(-2)$$

$$m = 5$$

Equation of tangent

$$y - (-5) = 5(x - (-2))$$

$$y + 5 = 5(x + 2)$$

$$y = 5x + 10 - 5$$

$$y = 5x + 5$$

$$y - 5x - 5 = 0$$

Equation of normal

$$y + 5 = -\frac{1}{5}(x + 2)$$

$$5y + 25 = -x - 2$$

$$5y + x + 25 + 2 = 0$$

$$5y + x + 27 = 0$$

5) $y = \frac{1}{x}$ at the point $(3, \frac{1}{3})$

$$y = x^{-1}$$

$$\frac{dy}{dx} = -\frac{1}{x^2}$$

$$\left. \frac{dy}{dx} \right|_{x=3} = -\frac{1}{(3)^2} = -\frac{1}{9}$$

Equation of tangent

$$y - \frac{1}{3} = -\frac{1}{9}(x - 3)$$

$$9y - 3 = -x + 3$$

$$9y + x - 3 - 3 = 0$$

$$9y + x - 6 = 0$$

Equation of normal

$$y - \frac{1}{3} = -\frac{1}{-\frac{1}{9}}(x + 3)$$

$$y - \frac{1}{3} = \frac{1}{1} \times \frac{9}{1} (x - 3)$$

$$y - \frac{1}{3} = 9(x - 3)$$

$$3y - 1 = 27x - 81$$

$$3y - 27x - 1 + 81 = 0$$

$$3y - 27x + 80 = 0$$