

1) $y = 2x^2$ at $(1, 2)$

$$m = \frac{dy}{dx} = \therefore \frac{dy}{dx} \Big|_{x=1} = 4(1) = 4$$

$$y - y_1 = m(x - x_1)$$

$$y - 2 = 4(x - 1)$$

$$y - 2 = 4(x - 1)$$

$$y - 2 = 4x - 4$$

$$y - 4x + 2 = 0 \text{ (which gives eqn of tangent)}$$

$$y - y_1 = -\frac{1}{m}(x - x_1)$$

$$y - 2 = -\frac{1}{4}(x - 1)$$

$$4y - 8 = -x + 1$$

$$4y + x - 9 = 0 \text{ (which gives eqn of the normal)}$$

2) $y = 3x^2 - 2x$ at $(2, 8)$

$$m = \frac{dy}{dx} = 6x - 2 \therefore \frac{dy}{dx} \Big|_{x=2} = 6(2) - 2 = 10$$

$$y - y_1 = m(x - x_1)$$

$$y - 8 = 10x - 20$$

$$y - 10x + 12 = 0 \text{ (which gives eqn of tangent)}$$

$$y = 8 = -\frac{1}{10}(x - 2)$$

$$10y - 80 = -x + 2$$

$$10y + x - 82 = 0 \text{ (which gives eqn of the normal)}$$

3) $y = \frac{x^3}{2}$ at $(-1, \frac{1}{2})$

$$m = \frac{dy}{dx} = \frac{3x^2}{2} \therefore \frac{dy}{dx} \Big|_{x=-1} = \frac{3}{2}(1) = \frac{3}{2}$$

$$y - y_1 = m(x - x_1)$$

$$y + \frac{1}{2} = \frac{3}{2}(x + 1)$$

$$2y + 1 = 3x + 3$$

$$2y - 3x - 2 = 0 \text{ (which gives eqn of tangent)}$$

$$\text{or tangent)}$$

$$y - y_1 = -\frac{1}{m}(x - x_1)$$

$$y + \frac{1}{2} = -\frac{2}{3}(x + 1)$$

$$3y + \frac{3}{2} = -2x - 2$$

$$6y + 4x + 7 = 0 \text{ (which gives eqn of the normal)}$$

4) $y = 1 + x - x^2$ at $(-2, -5)$

$$\frac{dy}{dx} = 1 - 2x \therefore \frac{dy}{dx} \Big|_{x=-2} = 1 - 2(-2) = 5$$

$$y - y_1 = m(x - x_1)$$

$$y - 5 = 5(x + 2)$$

$$y - 5x - 5 = 0 \text{ (which gives eqn of tangent)}$$

$$y + y_1 = \frac{1}{m}(x - x_1)$$

$$y + 5 = \frac{1}{5}(x + 2)$$

$$5y + 25 = x - 2$$

$$5y + x + 27 = 0 \text{ (which gives eqn of the normal)}$$

$$5.) y = 1/x = x^{-1} \text{ at } (3, 1/3)$$

$$\frac{dy}{dx} = -x^{-2}$$

$$\therefore \frac{dy}{dx} \Big|_{x=3} = \frac{-1}{(3)^2} = -\frac{1}{9}$$

$$y - \frac{1}{3} = -\frac{1}{9}(x - 3)$$

$$9y - 3 = -x + 3$$

$$9y + x - 6 = 0 \text{ (which gives eqn of the tangent)}$$

$$y - y_1 = m(x - x_1)$$

$$y - \frac{1}{3} = -\frac{1}{9}(x - 3)$$

$$y - \frac{1}{3} = -\frac{1}{9}x + \frac{1}{3}$$

$$3y - 1 = -x + 3$$

$$3y - 37x + 80 = 0 \text{ (which gives eqn of a normal)}$$