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DATE: 4/4/2020
DEPT: MECHATRONICS

Assignment

$$① \lim_{x \rightarrow 0} \frac{x - \cos x}{x} = \lim_{x \rightarrow 0} \left(1 - \frac{\cos x}{x} \right)$$

$$= \lim_{x \rightarrow 0} \frac{\frac{d}{dx}(1 - \cos x)}{\frac{d}{dx}x} = \frac{\frac{d(1)}{dx} - \frac{d(\cos x)}{dx}}{dx/dx}$$

$$= \frac{0 - (-\sin x)}{1} = \sin x$$

$$\therefore \lim_{x \rightarrow 0} \sin x = \sin 0 = 0$$

$$② y = -3 \tan 2x e^{3x} \quad \text{Let } u = -3 \tan 2x \\ v = e^{3x}$$

Product rule; $uv = u'v + v'u$

$$u' = +2 \sec^2 2x \quad v' = 3e^{3x}$$

$$\therefore \frac{dy}{dx} = 2 \sec^2 2x e^{3x} - 9e^{3x} \tan 2x$$

$$③ y = \cos 3x$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$$

$$\therefore f'(x) = \lim_{h \rightarrow 0} \frac{\cos 3(x+h) - \cos 3x}{h} \quad \text{Recall } \cos A - \cos B = -2 \sin \left(\frac{A+B}{2} \right) \sin \left(\frac{A-B}{2} \right)$$

$$\text{Recall; } \cos A - \cos B = -2 \sin \left(\frac{A+B}{2} \right) \sin \left(\frac{A-B}{2} \right)$$

$$A = 3(x+h) = 3x + 3h \quad B = 3x$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{-2 \sin\left(\frac{6x+3h}{2}\right) \sin\left(\frac{3h}{2}\right)}{h}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{-2 \sin\left(3x + \frac{3h}{2}\right) \sin\left(\frac{3h}{2}\right)}{h}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{-2 \sin\left(3x + \frac{3h}{2}\right) \times \sin\left(\frac{3h}{2}\right)}{h}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{-\sin\left(3x + \frac{3h}{2}\right) \times \sin\left(\frac{3h}{2}\right)}{h/2}$$

Multiply each term by $\frac{3}{3}$

$$f'(x) = \lim_{h \rightarrow 0} \frac{-\frac{3}{3} \sin\left(3x + \frac{3h}{2}\right) \times \frac{3}{3} \sin\left(\frac{3h}{2}\right)}{\frac{3h}{2}}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{-\sin\left(3x + \frac{3h}{2}\right) \times 3}{1} = -(\sin 3x) \times 3$$

$$\therefore f'(x) = -3 \sin 3x$$

$$(4) \quad g(x) = -3(x) \quad \therefore g(5) = -3(5) = -15$$

$$f(5) = 2(5)^3 - g(5) = 250 - 35 = 215$$

$$(f-g)(5) = 215 - 15 = 200$$

$$(5) \quad g(x) = 2x + 3 \quad f(x) = 4x^2 + 2$$

$$f(g(x)) = 4(2x+3)^2 + 2 = 4(4x^2 + 12x + 9) + 2$$

$$= 16x^2 + 48x + 38$$

$$\textcircled{6} \quad x^2 + 2xy + y^2 = 1020$$

$$2x + 2y + \frac{2x dy}{dx} + \frac{2y dy}{dy} = 0$$

$$(2x + 2y) \frac{dy}{dx} = -(2x + 2y)$$

$$\frac{dy}{dx} = \frac{-(2x + 2y)}{(2x + 2y)} = -1$$

$$\therefore \frac{dy}{dx} = -1$$

$$\textcircled{7} \quad y = x^2 \cos x \quad \text{let} \quad u = x^2 \quad u' = 2x$$

$$v = \cos x \quad v' = -\sin x$$

Product rule; $u = x^2 \quad v = \cos x$

$$u'v + v'u$$

$$\therefore \frac{dy}{dx} = 2x \cos x - x^2 \sin x$$