

①  $y - 3x - 2 = 0$  &  $3y + x + 9 = 0$  (perpendicular when  $m_1 m_2 = -1$ )  
 where  $m = \frac{dy}{dx}$

$$y_1 = 3x + 2$$

$$\frac{dy}{dx} = 3$$

$$m_1 = 3$$

$$y_2 = -\frac{x}{3} + 9$$

$$\frac{dy}{dx} = -\frac{1}{3}$$

$$m_2 = -\frac{1}{3}$$

they are perpendicular as  $\frac{dy}{dx}$  is negative inverse of the other  
 $m_1 = -\frac{1}{m_2}$

②  $3y - 4 = 2x + 3$

$$3y = 2x + 3 + 4$$

$$3y = 2x + 7$$

$$y = \frac{2x + 7}{3}$$

$$\frac{dy}{dx} = \frac{2}{3}$$

$$m_1 = \frac{2}{3}$$

$y - 5 = x + 6$

$$y = x + 6 + 5$$

$$y = x + 11$$

$$\frac{dy}{dx} = 1$$

$$m_2 = 1$$

they are not perpendicular  $m_1 \neq -\frac{1}{m_2}$

③  $x^2 + y^2 + 3xy - 4 = 0$   $(x_1, y_1)$   
 $(1, 2)$

$$2x + 2y \frac{dy}{dx} + 3 \left[ y + x \frac{dy}{dx} \right] - 0 = 0$$

$$2x + 2y \frac{dy}{dx} + 3y + 3x \frac{dy}{dx} = 0$$

$$2y \frac{dy}{dx} + 3x \frac{dy}{dx} = -2x - 3y$$

$$\frac{dy}{dx} \left[ \frac{2y+3x}{2y+3x} \right] = \frac{-2x-3y}{2y+3x}$$

$$\frac{dy}{dx} = - \frac{[2x+3y]}{2y+3x} = - \frac{[2(1)+3(2)]}{2(2)+3(1)}$$

$$\frac{dy}{dx} = - \frac{[2+6]}{4+3} = \frac{-8}{7} = m_1$$

(a) equation of the tangent

$$m_1 = m_2$$

$$\frac{y-2}{x-1} = \frac{-8}{7}$$

$$7y - 14 = -8x + 8$$

$$7y + 8x - 14 - 8 = 0$$

$$7y + 8x - 22 = 0$$

(b) equation of the normal  $m_2 = \frac{-1}{m_1} = \frac{-1}{-8/7} = \frac{7}{8}$

$$\frac{y-2}{x-1} = \frac{7}{8}$$

$$8y - 16 = 7x - 7$$

$$8y - 7x - 16 + 7 = 0$$

$$8y - 7x - 9 = 0$$