

$$1) \begin{aligned} y - 2x - 2 &= 0 \quad \text{and} \quad 3y + x + 9 = 0 \\ \text{let } T &= y - 2x - 2 = 0, \quad y = 2x + 2 \\ \text{Gradient, } M_1 &= \frac{dy}{dx} = 2 \end{aligned}$$

$$M_1 = 2$$

$$\text{let } U = 3y + x + 9 = 0$$

$$\frac{dy}{dx} = -\frac{x+9}{3}$$

$$y = -\frac{x}{3} - 3$$

$$\text{Gradient, } M_2 = \frac{dy}{dx} = -\frac{1}{3}$$

$$M_1 M_2 = -1$$

$$2 \times -\frac{1}{3} = -1$$

Therefore, $y - 2x - 2 = 0$ is perpendicular to $3y + x + 9 = 0$

$$2) \quad 3y - 4 = 2x + 3 \quad \text{and} \quad y - 5 = x + 6$$

$$\text{let } E = 3y - 4 = 2x + 3$$

$$\frac{dy}{dx} = \frac{2x+7}{3}$$

$$y = \frac{2}{3}x + \frac{7}{3}$$

$$\text{Gradient, } M_1 = \frac{dy}{dx} = \frac{2}{3}$$

$$\text{let } F = y - 5 = x + 6$$

$$y = x + 1$$

$$\text{Gradient, } M_2 = \frac{dy}{dx} = 1$$

$$M_1 M_2 = -1$$

$$\frac{2}{3} \times 1 \neq -1$$

Therefore, $3y - 4 = 2x + 3$ and $y - 5 = x + 6$ is not perpendicular
P.Q.C.1)

2) $x^2 + y^2 + 8xy - 11 = 0$ at point (1, 2)

$$2x + 2y \frac{dy}{dx} + 2(x \cdot 8y/x + y \cdot 1) - 0 = 0$$

$$2x + 2y \frac{dy}{dx} + 2x \cdot 8y/x + 2y = 0$$

$$\frac{dy}{dx} = \frac{-2x - 2y}{2y + 8x}$$

at point, $M = dy/dx = \frac{-2x - 2y}{2y + 8x}$

when $x = 1$ and $y = 2$

$$M = -\left[\frac{2(1) + 2(2)}{2(1) + 8(1)} \right]$$

$$M = \frac{-(2+4)}{4+8} = -\frac{6}{12} = -\frac{1}{2}$$

$$M = -\frac{1}{2}$$

Equation of the tangent to a curve

$$y - y_1 = M(x - x_1)$$

$$y - 2 = -\frac{1}{2}(x - 1)$$

$$y - 2 = -\frac{1}{2}x + \frac{1}{2}$$

$$\frac{1}{2}y + 2 = -\frac{1}{2}x + \frac{1}{2}$$

$$\frac{1}{2}y + \frac{3}{2} = -\frac{1}{2}x + \frac{1}{2}$$

$$\frac{1}{2}y + \frac{3}{2} + \frac{1}{2} = 0$$

Equation of the normal to a curve

$$M_1 M_2 = -1$$

$$-\frac{1}{2} + M_2 = -1$$

$$M_2 = -1 \times -\frac{1}{2} = \frac{1}{2}$$

$$y - y_1 = M(x - x_1)$$

$$y - 2 = \frac{1}{2}(x - 1)$$

$$y - 2 = \frac{1}{2}x - \frac{1}{2}$$

$$\frac{1}{2}y + 2 = \frac{1}{2}x - \frac{1}{2}$$

$$\frac{1}{2}y + \frac{5}{2} = \frac{1}{2}x - \frac{1}{2}$$

$$\frac{1}{2}y + \frac{5}{2} + \frac{1}{2} = 0$$

$$\frac{1}{2}y + \frac{3}{2} = 0$$

$$\frac{1}{2}y = -\frac{3}{2}$$

$$y = -3$$

$$y = -3$$