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Examine whether or not these pair of lines are perpendicular to each other.

1 $y - 3x - 2 = 0$ and $3y + x + 9 = 0$

$$y - 3x - 2 = 0$$

$$y = 3x + 2$$

$$y = m_1x + c$$

$$m_1 = 3$$

$$3y + x + 9 = 0$$

$$3y = -x - 9$$

$$y = -\frac{1}{3}x - 3$$

$$y = m_2x + c$$

$$m_2 = -\frac{1}{3}$$

$$m_1 m_2 = 3 \times -\frac{1}{3}$$

$$m_1 m_2 = -1$$

∴ The lines $y - 3x - 2 = 0$ and $3y + x + 9 = 0$ are perpendicular to each other.

2 $3y - 4 = 2x + 3$ and $y - 5 = x + 6$

$$3y - 4 = 2x + 3$$

$$3y \cancel{-4} = 2x + 3 + 4$$

$$3y = 2x + 7$$

$$y = \frac{2}{3}x + \frac{7}{3}$$

$$y = m_1 x + c$$

$$m_1 = \frac{2}{3}$$

$$y - 5 = x + 6$$

$$y = x + 6 + 5$$

$$y = x + 11$$

$$y = m_2 x + c$$

$$m_2 = 1$$

For 2 lines to be perpendicular, $m_1 m_2 = -1$

$$m_1 m_2 = \frac{2}{3} \times 1$$

$$m_1 m_2 = \frac{2}{3}$$

$$m_1 m_2 \geq -1$$

\therefore The lines $3y - 4 = 2x + 3$ and $y - 5 = x + 6$ are not perpendicular to each other.

3 Find the equations of the tangent and normal to the line $x^2 + y^2 + 3xy - 11 = 0$ at the point $x_r = 1$ and $y = 2$

$$x^2 + y^2 + 3xy - 11 = 0$$

$$\frac{d}{dx}(x^2 + y^2 + 3xy - 11) = 0$$

$$2x + 2y \frac{dy}{dx} + 3(y) + x \frac{dy}{dx} - 0 = 0$$

$$2x + 2y \frac{dy}{dx} + 3y + 3x \frac{dy}{dx} = 0$$

$$2y \frac{dy}{dx} + 3x \frac{dy}{dx} = -2x - 3y$$

$$\frac{dy}{dx} = \frac{-2x - 3y}{2y + 3x}$$

3

$$m = \frac{dy}{dx} \Big|_{x=1, y=2}$$

$$m = \frac{-2(1) - 3(2)}{2(1) + 3(1)}$$

$$m = \frac{-2 - 6}{4 + 3}$$

$$m = -\frac{8}{7}$$

a The equation of the tangent

$$y - y_1 = m(x - x_1)$$

$$y - 2 = -\frac{8}{7}(x - 1)$$

$$7(y - 2) = -8(x - 1)$$

$$7y - 14 = -8x + 8$$

$$7y = -8x + 8 + 14$$

$$7y = -8x + 22$$

OR

$$7y + 8x - 22 = 0$$

b The equation of the normal:

$$y - y_1 = -\frac{1}{m}(x - x_1)$$

$$y - 2 = -1/(-\frac{8}{7})(x - 1)$$

$$y - 2 = \frac{7}{8}(x - 1)$$

$$8(y - 2) = 7(x - 1)$$

$$8y - 16 = 7x - 7$$

$$8y = 7x - 7 + 16$$

$$8y = 7x + 9$$

OR

$$8y - 7x - 9 = 0$$