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16/ENG07/024 C/O

PETROLEUM ENGINEERING

PTE 314. HEAT AND MASS TRANSFER

Question

In order to avoid pressure build up gas at atmospheric pressure in a pipe, is vented to atmosphere through a pipe of 3mm diameter and 20m length. Determine the mass of the gas diffusing out and mass of air diffusing in per hour. Assume  $D = 0.28 \times 10^{-4} \text{ m}^2/\text{s}$ ,  $M = 17 \text{ kg/kg mole}$

Solution.

$$N_a = \frac{M_a}{M} \dots (i)$$

$$P_{a1} = 1 \text{ atm} = 1.013 \times 10^5 \text{ Nm}^{-2}$$

$$P_{a2} = 0 \text{ [since the gas is vented to the atmosphere]}$$

$$L = 20 \text{ m}$$

$$d = 3 \text{ mm} \approx \frac{3}{1000} = 0.003 \text{ m}$$

$$A = \frac{\pi d^2}{4} \Rightarrow \frac{\pi}{4} (0.003)^2 = 7.068 \times 10^{-6} \text{ m}^2$$

$$\text{Molar Mass, } M = 17 \text{ kg/kg mol}$$

$$R = 8315 \text{ J/kg mol K}$$

$$D = 0.28 \times 10^{-4} \text{ m}^2/\text{s}$$

Using the equimolar counter diffusion equation;

$$\frac{N_a}{A} = \frac{D}{R\bar{T}} \cdot \frac{P_{a1} - P_{a2}}{L} \Rightarrow N_a = \frac{DA}{R\bar{T}} \cdot P_{a1} - P_{a2}$$

where  $\bar{T}$  is the temperature in absolute unit i.e  $^{\circ}\text{K}$

$$\therefore N_a = \frac{DA}{R} \cdot \frac{P_{a1} - P_{a2}}{L}$$

Substituting equation (i)

$$\frac{M_a}{M} = \frac{DA}{R} \cdot \frac{P_{a1} - P_{a2}}{L}$$

$$M_a = \frac{D \cdot A}{R} \cdot \frac{P_{a1} - P_{a2}}{L} \times M$$

where  $M_a$  is the mass of gas diffusing out in kg ls

$$m_a = \frac{DA}{R} \cdot \frac{P_{a1} - P_{a2}}{L} \times M (3000) \dots \text{kg/hr}$$

$$M_a = \frac{(0.28 \times 10^{-4}) \times (7.068 \times 10^{-6})}{8315} \times \frac{(1.013 \times 10^{-5} - 0) \times (17 \times 3000)}{20}$$

$$= 7.38 \times 10^{-6} \text{ kg/hr}$$

b Mass of air diffusing in ( $M_{ai}$ )

Recall  $\frac{N_a}{A} = -\frac{N_b}{A}$

$$\therefore N_a = -N_b$$

$$N_b = -N_a$$

$$= -7.38 \times 10^{-6}$$

$$\text{Mole of air} = \frac{-7.38 \times 10^{-6}}{17}$$

$$= -4.34 \times 10^{-7}$$

$$\text{Mass of air} = -4.34 \times 10^{-7} \times 28.97$$

$$= -1.26 \times 10^{-5} \text{ kg/hr}$$